

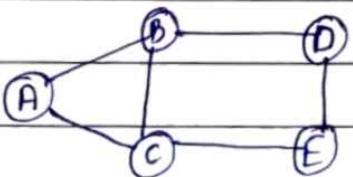
## \* Graph

- A graph  $G$  is a set of vertices ( $V$ ) and a set of edges ( $E$ ).
- The set  $V$  is a finite, nonempty set of vertices.
- The set  $E$  is a set of pairs of vertices representing edges.

$$G = (V, E)$$

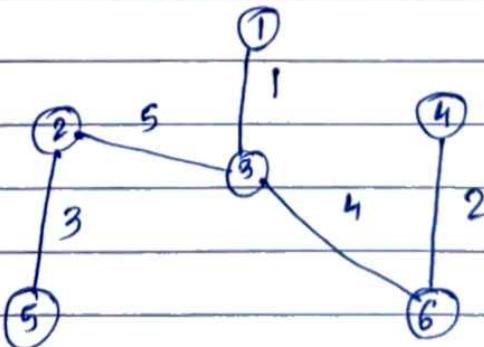
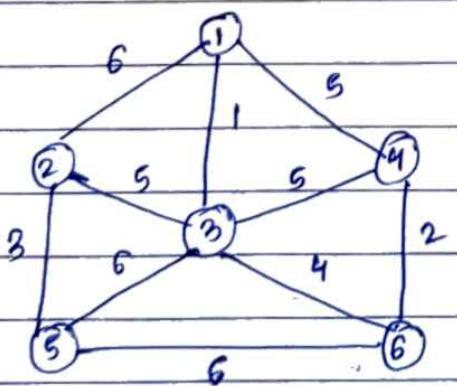
$V(G)$  = Vertices of graph  $G$

$E(G)$  = Edges of graph  $G$



## \* Minimum spanning tree

- With applications of weighted graphs, it is often necessary to find a spanning tree for which the total weight of the edges in the tree is as small as possible.
- Such a spanning tree is called a minimal spanning tree or minimum cost spanning tree.



\* ~~Prim's Algorithm~~

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- Let the graph  $G = (V, E)$  has  $n$  vertices.

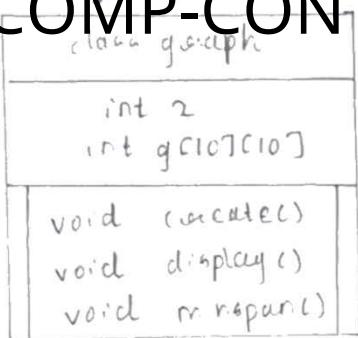
Step 1: choose a vertex  $v_i$  of  $G$ . Let  $V_T = \{v_i\}$  and  $E_T = \{\}$ .

Step 2: choose a nearest neighbour  $v_j$  of  $v_i$  that is adjacent to  $v_i$ ,  $v_j \in V_T$  and for which the edge  $(v_i, v_j)$  does not form a cycle with members of  $E_T$ . Add  $v_j$  to  $V_T$  and add  $(v_i, v_j)$  to  $E_T$ .

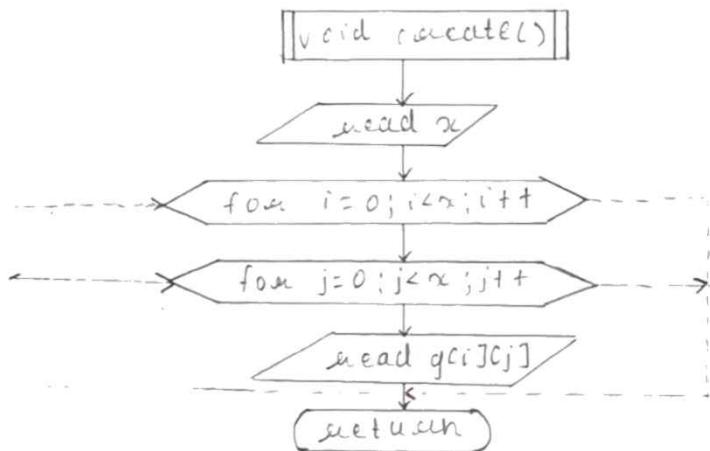
Step 3: Repeat step 2 until  $|E_T| = n-1$ . Then  $V_T$  contains all  $n$  vertices of  $G$  and  $E_T$  containing the edges of the minimum cost spanning tree of  $G$ .

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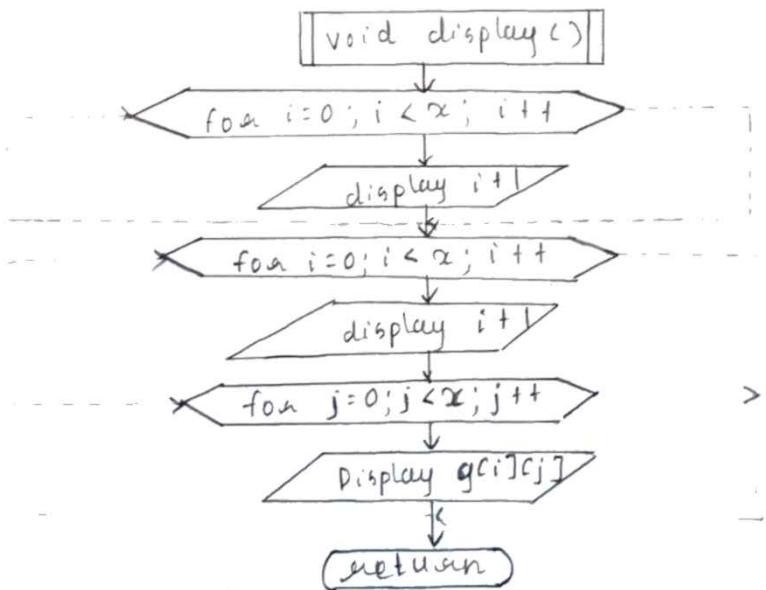
flowchart for class graph

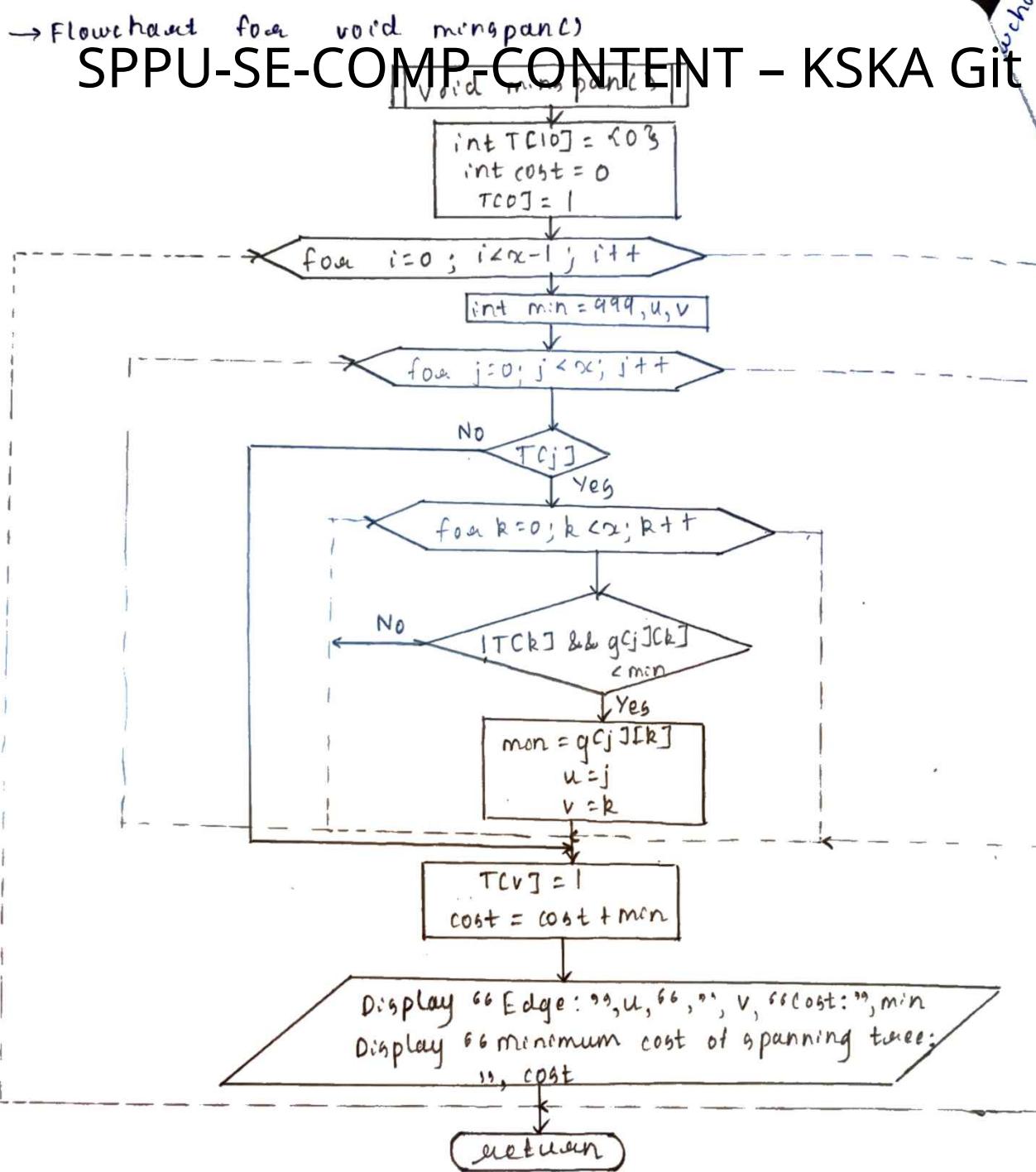


→ flowchart for void create()



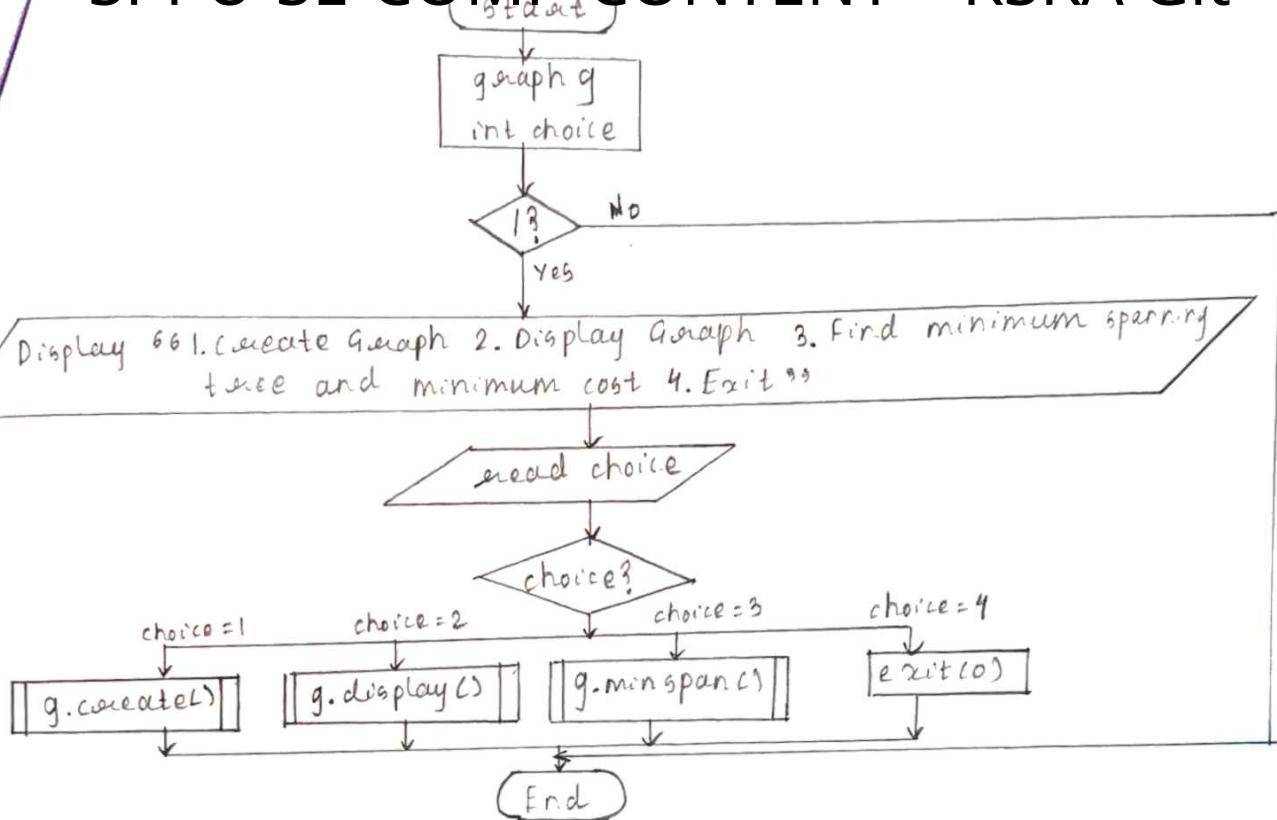
→ flowchart for void display()





which set four int main()

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→ Pseudocode for class graph

1. Declare int x  
    int g[10][10]
2. Declare function create()  
    function display()  
    function minspan()

•

→ Pseudocode for ~~class~~ void create()

1. Display "Enter number of nodes: "

read x

3. for i=0; i<x; i++ do

begin

    for j=0; j<x; j++ do

begin

        Display "Enter cost of graph: "

        read g[i][j]

    end

end

4. return

→ Pseudocode for void display()

1. for i=0; i<x; i++ do

begin

    display i+1

end

2. for i=0; i<x; i++ do

begin

    display i+1

    for j=0; j<x; j++ do

begin

        display g[i][j]

end

end

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3. Screenshot

→ Pseudocode for void mingspan()

1. declare int T[10] = 203

2. initialize cost = 0

3. initialize T[0] = 1

4. for i=0; i < n-1; i++ do

begin

    initialize min = 999, u, v

    for j=0; j < n; j++ do

        begin

            if T[j] then

                for k=0; k < n; k++ do

                    begin

                        if !T[k] and g[j][k] < min then

                            initialize min = g[j][k]

                            u = j

                            v = k

                        end

            end

        initialize T[v] = 1

        cost = cost + min

        Display "Edge: ("", u, "", ", ", v, ") cost: ", min

        Display "Minimum cost of spanning tree: ", cost

    end

5. return

→ Pseudocode for int main()

1. Start

2. Create object g

3. Declare int choice

4. while (1) do

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begin

Display @@ 1. Create Agraph 2. Display Agraph 3. Find  
minimum spanning tree and minimum  
cost 4. Exit "

read choice

(switch choice)

case 1:

call function g.create()

break

case 2:

call function g.display()

break

case 3:

call function g.minspan()

break

case 4:

exit()

break

default :

Display @@ Enter a valid choice"

break

end

5 End

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Q1. Suppose we have an undirected graph with weights that can be either positive or negative. Do Prim's and Kruskal's algorithm produce an MST for such a graph?

- Ans. Yes, negative edge weights are no problem for Prim's and Kruskal's algorithm.
- Both of these algorithms are greedy algorithms and the reason why the greedy approaches to finding the MST work is that you can always get a better ST of there is an unused edge that has a lower weight than any edge on the cycle that would be created by adding it on the ST.
  - This principle holds for both positive and negative edge weights.

Q2. Can a graph have more than one spanning tree?

Ans. A connected graph can have more than one spanning tree.

- All spanning trees must contain the same number of vertices as of graph, and the number of edges must be equal to  $|V| - 1$ .
- The spanning tree must not contain any cycle.
- A spanning tree is a subgraph of a graph in which all the vertices are connected and it does not have any loops.
- Therefore, a graph can have multiple spanning trees.

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Q3. State the difference between Prim's and Kruskal's algorithm.

Ans:

Kruskal's

Prim's

1. Select the shortest edge in a network.

2. Select the next shortest edge which does not create a cycle.

3. If graph is created using adjacency matrix, time complexity  $\rightarrow O(n^2)$

4. If graph is created using list, Time complexity  $\rightarrow O(n^2) + O(E \cdot \log n) = O(n^2)$

5. Kruskal's algorithm performs better for sparse graph

1. Select any vertex

2. Select the shortest edge connected to the vertex

3. If graph is created using adjacency matrix, time complexity  $\rightarrow O(n^2)$

4. If graph is created using list, Time complexity  $\rightarrow O(E \cdot \log n)$

5. Prim's algorithm is comparatively less efficient for a sparse graph.