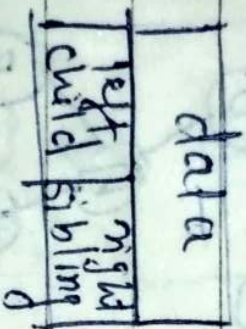


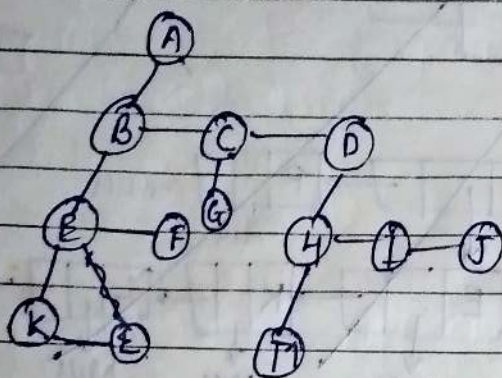
Q Left child - Right Sibling Representation :-



Left child - right sibling node structure.

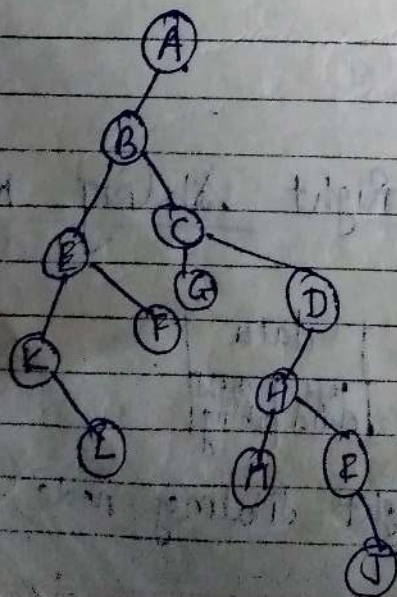
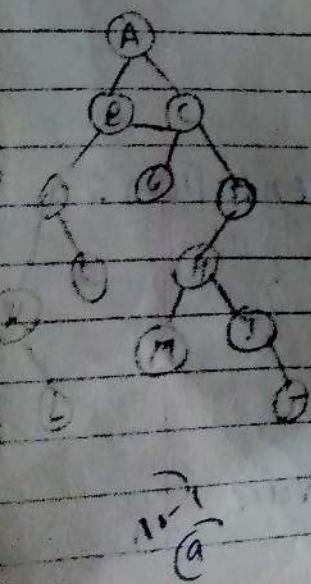
left child - right sibling representation:-

- To convert the tree into this representation, we have ^{shown} every node has at most one leftmost child & at most one ~~one~~ closest right sibling.

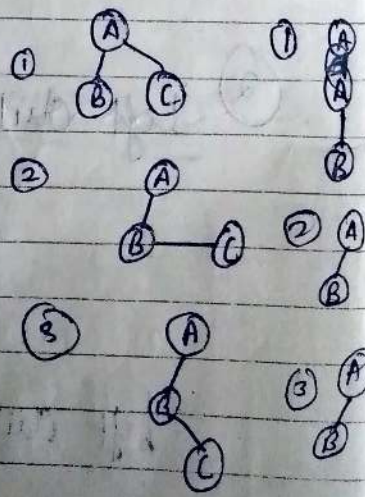


③ Representation as a Degree-Two Tree:-

- we simply rotate the right sibling pointers ^(A) clockwise in a ~~left~~ by 45° .



example:-



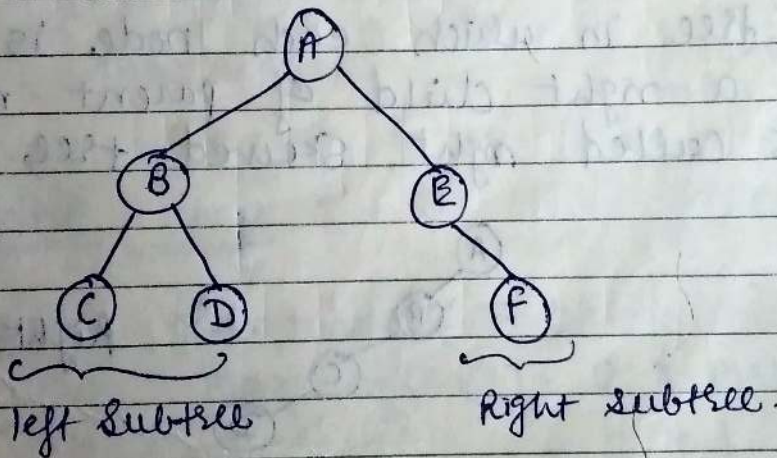
* Binary Trees :-

Definition :-

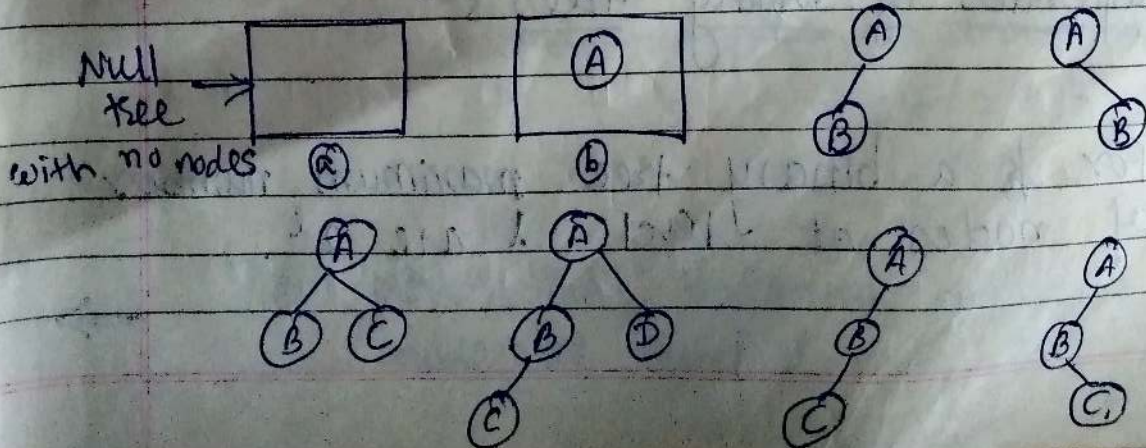
A binary tree is a finite set of nodes that either is empty or consists of a root and two disjoint binary trees called the left subtree and the right subtree.

- A binary tree is a tree in which no node can have more than two subtrees.

or a node can have ~~2~~ zero, one or two subtrees.



Collection of Binary Trees :-

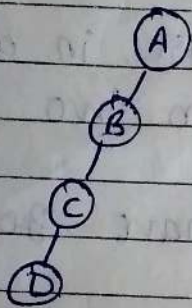


* Properties of Binary trees :-

① Left and Right skewed trees :-

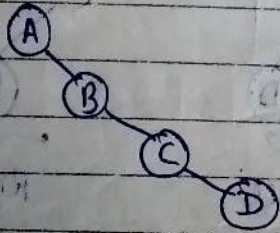
- The tree in which each node is attached as a left child of parent node then it is left skewed tree.

- ~~The tree~~



left skewed tree.

→ The tree in which each node is attached as a right child of parent node then it is called right skewed tree.



Right skewed tree.

Properties of Binary trees :-

① For a binary tree maximum number of nodes at level l are 2^l .



proof:- Induction Base :

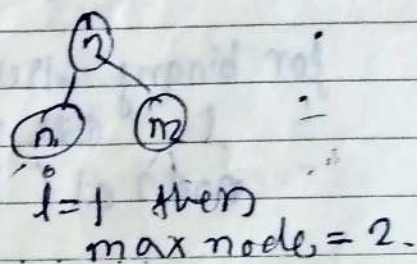
As we know, root node is a unique node present at 0th level.

That means, if $l=0$, maximum no. of nodes are 2^l i.e. $2^0 = 1$

The binary tree is a tree in which each node has maximum two nodes.

Hence if level $m=1$ then maximum nodes are, $2^1 = 2^1 = 2$.

(n)
 $l=0$ then
max node = 1



Inductive step :

As, $\text{max_nodes}(0) = 1$.

$$\text{max_nodes}(1) = 2 * \text{max_nodes}(0)$$

$$= 2 * 1 = 2$$

$$\text{" (2) } = 2 * \text{max_nodes}(1)$$

$$= 2 * 2 = 4$$

\therefore

So

$$\text{max_nodes}(k) = 2 * \text{max_nodes}(k-1)$$

$$= 2 * (2 * (2 * \dots * (2 * \text{max_nodes}(0))))$$

$$= 2^k$$

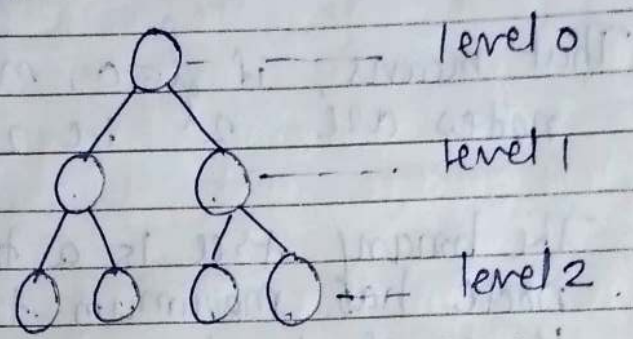
This proves that maximum number of nodes at level l are 2^l .

full binary tree = is a tree in which every node other than the leaves (strictly binary tree) has 2 children.

② A full binary tree of height h has exactly $(2^{h+1} - 1)$ nodes.

→ Induction Basis :-

$$\begin{aligned} (2^{3-1} - 1) &= 7 \\ (2^{0-1} - 1) &= 1 \end{aligned}$$



Height of a given tree is $h = 3$.

for binary tree, total no. of nodes at level l are 2^l . In above figure, total nodes at level 0 is 1 & 2 are 4

Thus the total no. of nodes in the given binary tree are,

$$\begin{aligned} \text{total nodes} &= 2^0 + 2^1 + 2^2 + \dots + 2^h \\ &= \sum_{i=0}^h 2^i \end{aligned}$$

If height $h = 1$,

then $2^{h-1} = 2^0 = 1$ ie root node.

height $h = 2$,

then $2^{h-1} = 2^1 = 2$ ie 2 nodes.

Induction hypothesis :

Assume total nodes $\bar{=}$ $2^{h-1} - 1$ for a full binary tree.

Inductive step :

Now a tree T has 2 subtrees T_L & T_R .
 height of subtrees ~~is~~ is $h-1$.

Hence, $T = T_L + T_R$.

total node = total node of $(T_L) + \text{total node}(T_R) + 1$.

$$T = (2^{h-1} - 1) + (2^{h-1} - 1) + 1$$

$$T = 2 \cdot 2^{h-1} - 1$$

$$T = 2^h - 1$$

Thus, a full binary tree of a given height h has $2^h - 1$ nodes is proved.

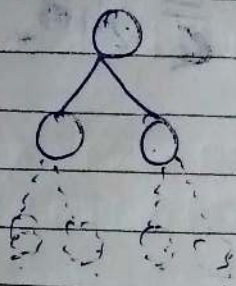
③ In a binary tree the no. of external nodes is one more than the no. of internal nodes. i.e. $e = i + 1$.

Proof:- It is true for one node:



$i = 1$
 $e = 1 + 1 = 2$

540416
 It is also true for 3 nodes :-



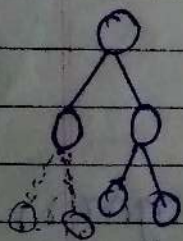
$i = 3$
 $e = 3 + 1 = 4$

Induction hypothesis :-

Assume it is also true with up to n nodes.

Assume true for a tree with n nodes
 $(e = i + 1)$. Now we want to add
 new external nodes.

→ Inductive step :-



when we add two external nodes then ~~two~~ old external becomes internal, so we have,

$$e_{\text{new}} = (e - 1) + 2$$

$$= e + 1$$

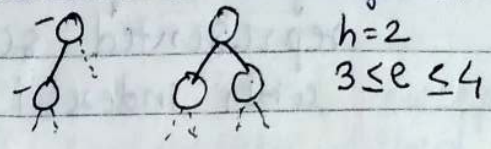
$$= (i + 1) + 1 = i + 2$$

$$i_{\text{new}} = ~~i + 1~~ i + 1$$

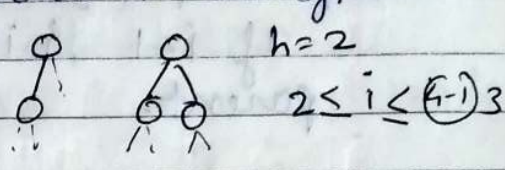
hence $e_{\text{new}} = i_{\text{new}} + 1$



④ The number of external nodes e satisfies, $(h+1) \leq e \leq 2^h$.



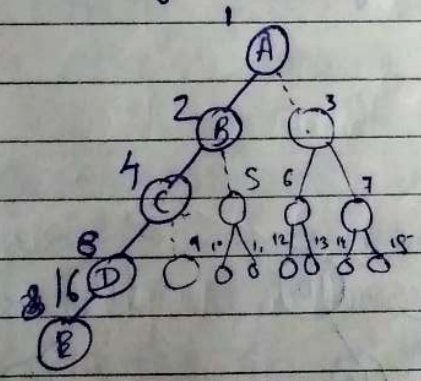
⑤ The number of internal nodes i satisfies, $h \leq i \leq 2^h - 1$.



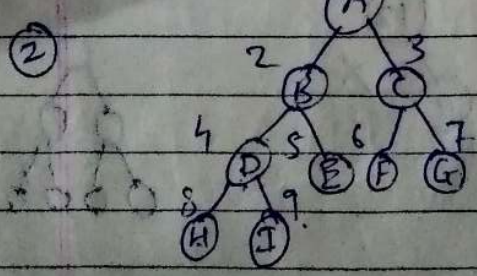
* Binary Tree Representation

- ① ~~Array~~ Array Representation.
- ② Linked Representation.

① Array Representation :-



0	-
1	A
2	B
3	-
4	C
5	-
6	B
7	-
8	D
...	...
16	E



1	-
2	A
3	B
4	C
...	...
9	I

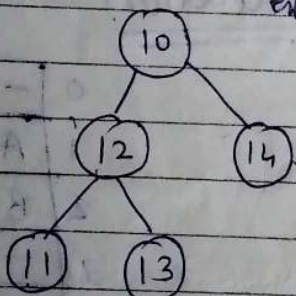
① If a complete binary tree with n nodes is represented sequentially, then for any node with index i , $1 \leq i \leq n$, we have:

1) parent (i) is at $\lfloor i/2 \rfloor$ if $i \neq 1$.
 If $i=1$, i is at the root and has no parent.

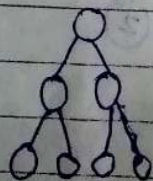
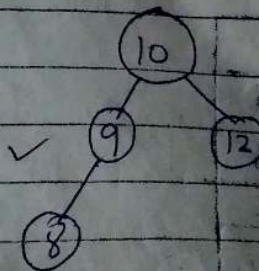
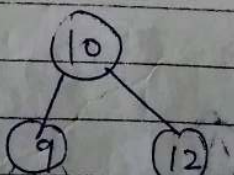
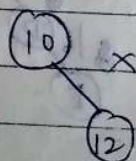
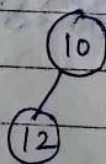
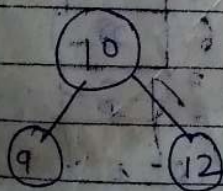
2) left child (i) is at $2i \leq n$. If $2i > n$ then i has no left child.

3) right child (i) is at $2i+1 \leq n$. If $2i+1 > n$, then i has no right child.

Full Binary tree: Each node has exactly 0 or 2 children



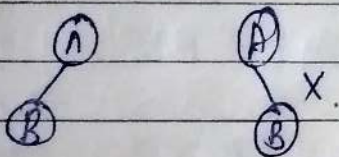
complete BT:



* Complete Binary tree :-

A binary tree in which every level, except possibly the deepest is completely filled.

and
At depth n , the height of the tree, all nodes must be as far left as possible.

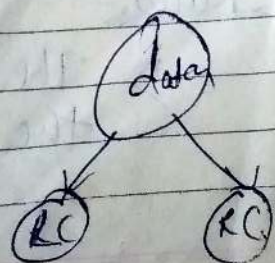
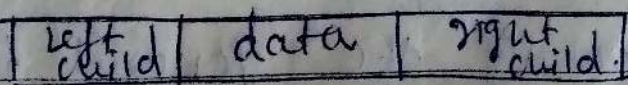


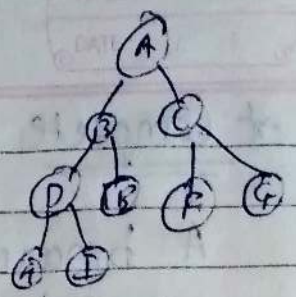
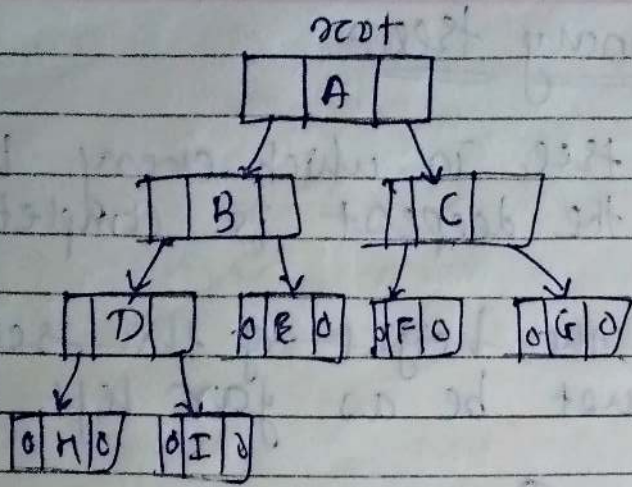
* Linked Representation :-

→ Array representation is good for complete binary trees, it is wasteful for many other binary trees.

→ Insertion and deletion of nodes from the middle of a tree require the movement of potentially many nodes to reflect the change in level no. of these nodes.

- So these problems are overcome by using linked representation.





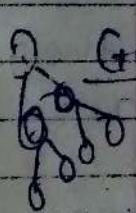
Struct node

```

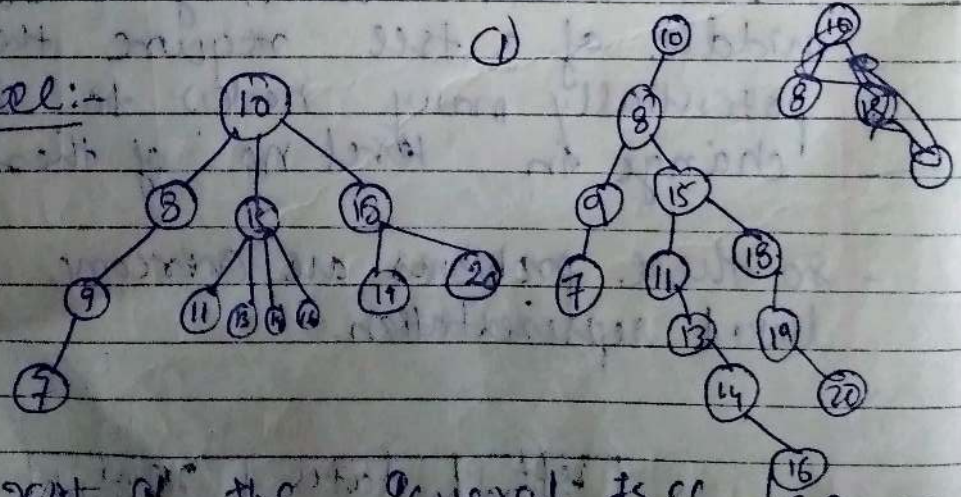
{
  int data;
  node *left;
  node *right;
};

```

* Converting tree to Binary tree:-



General tree:-

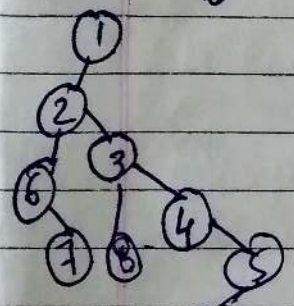
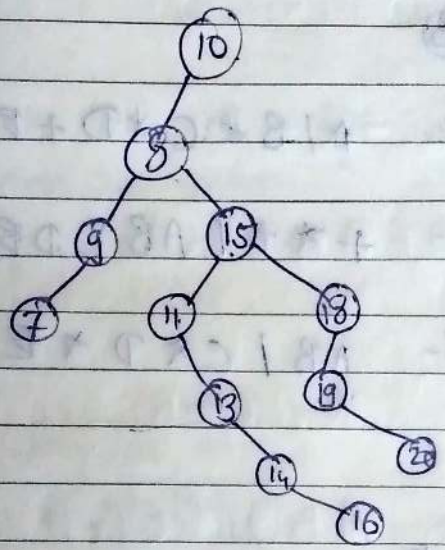
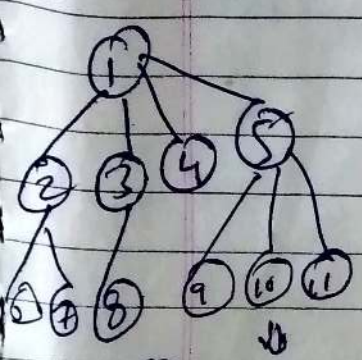


Rules:-

1) The root of the general tree becomes the root of the binary tree.

- 2) find the first child node of the node
attach it as a left child to the current node in binary tree.
- 3) The right siblings can be attached as a right child of that node.

2)

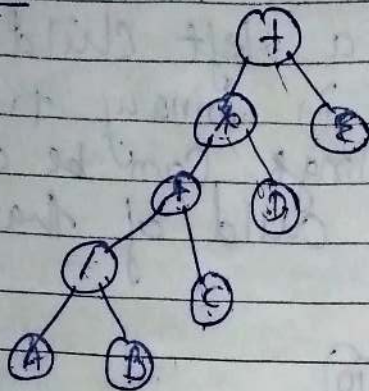


* Binary tree traversals :-

→ Three important traversal :- ~~LRV~~, ~~LVR~~, ~~ALV~~
 left-root-right }
 left-right-root } traverse left
 root-left-right } before-right.

- Inorder - left-root-right.
- preorder - root-left-right.
- post order - left-right-root.

example:-



① Inorder :- A/B*C*D+E

② preorder :- +**/ABCDE

③ postorder :- AB/C*D*E+

* Creation of Binary tree :-

```
class tree
{
    int data;
    tree *lptr;
    tree *rptr;
public:
    tree *create(int);
    tree *insert(int, tree *);
};

tree * tree::create(int x)
{
    tree *p;
    p = new node;
    if (p == NULL)
    {
```

```

p -> data = x;
p -> lptr = null;
p -> rptr = Null;
return p;
}

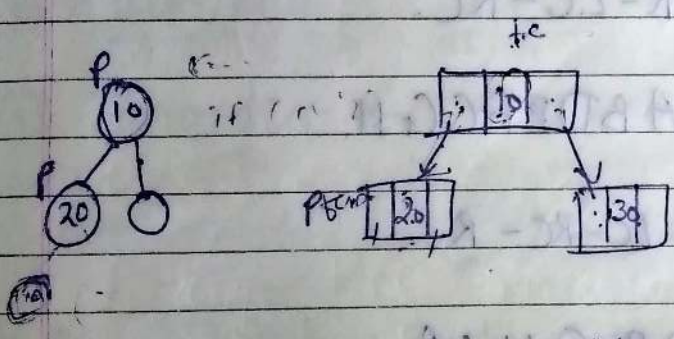
```

tree * tree :: insert(int x, tree * root)

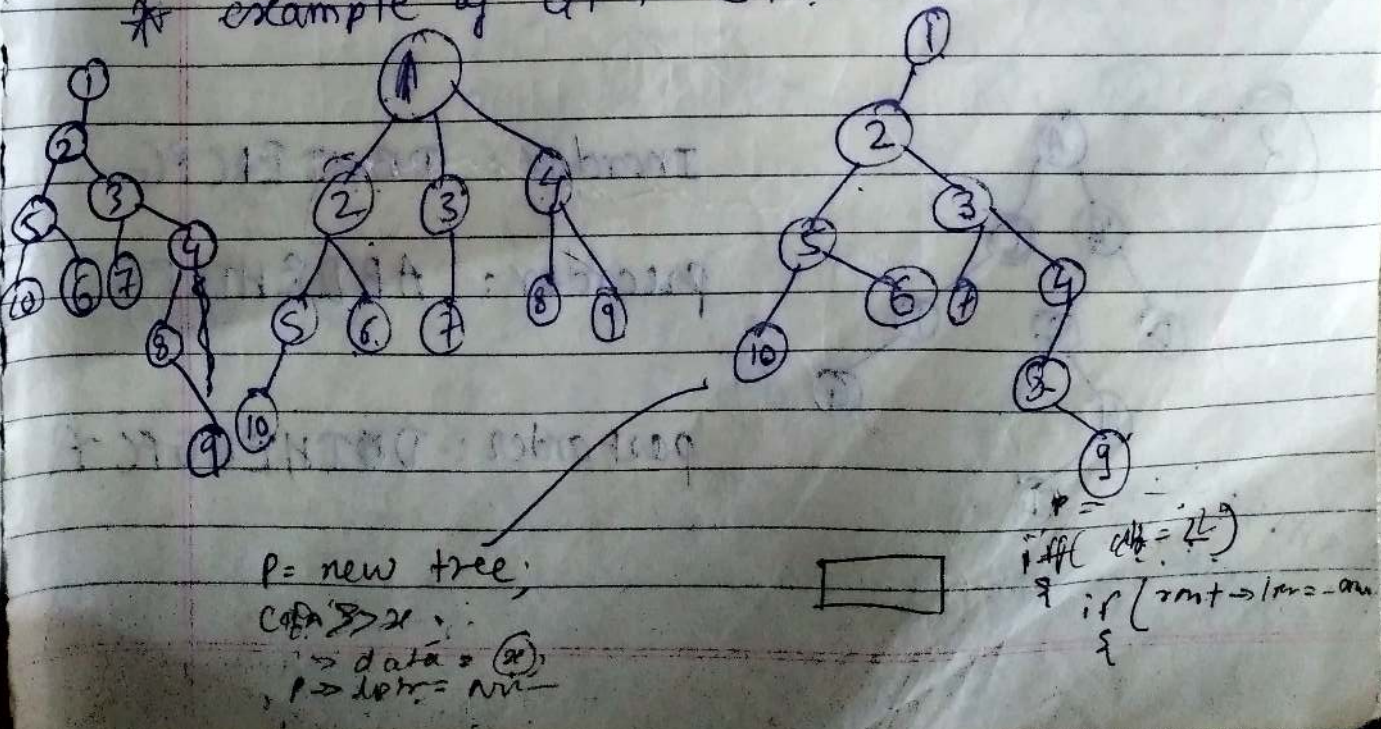
```

{
tree * p; * temp;
temp = root;
p = new tree;

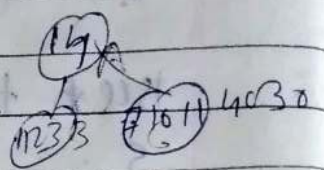
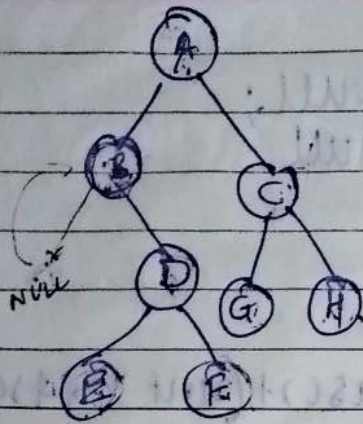
```



* example of GT to BT :-

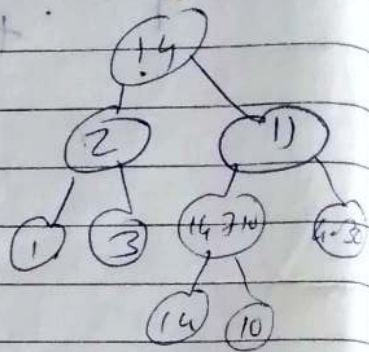


example:-



① Inorder:- RL-R-RC

→ BEDFA GCH



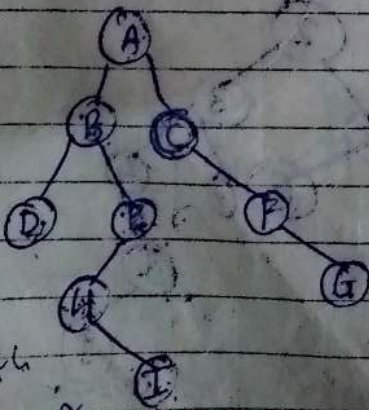
② preorder:- R-LC-RC

~~AB~~ ABDEF CGH

③ postorder:- LC-RC-R

E.FDB G HCA.

②

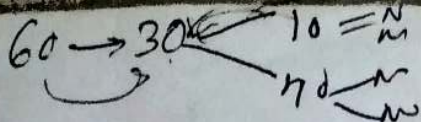


Inorder :- DBHIEACFG

preorder :- ABDEHICFG

post order :- D I H E B G F C A

DBHIEACFG
D I H E B G F C A



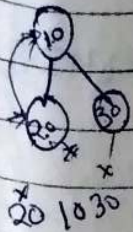
void inorder (tree *root) ← address of the root node is passed.

{
if (root != NULL)

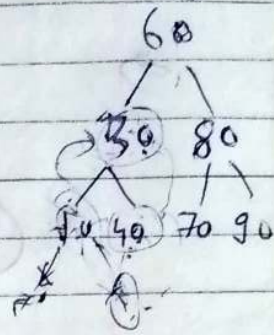
inorder (root → left);

cout << " " << T → data;

inorder (root → right);



60 30 10



60 → 30 - 10
10 20 40 70 90
Fio

Create Binary tree from following traversal:-

① Inorder :- E A C K P H D B G

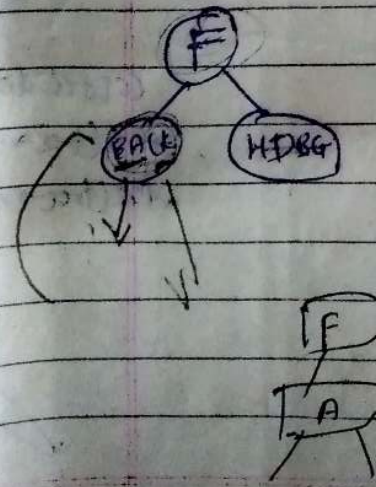
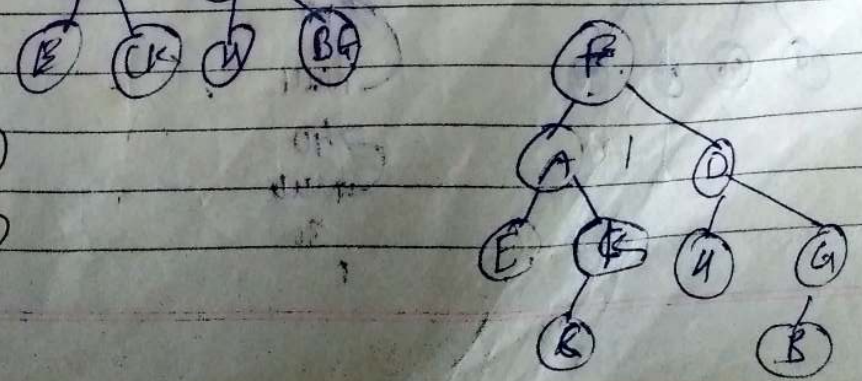
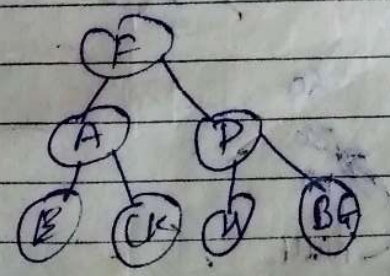
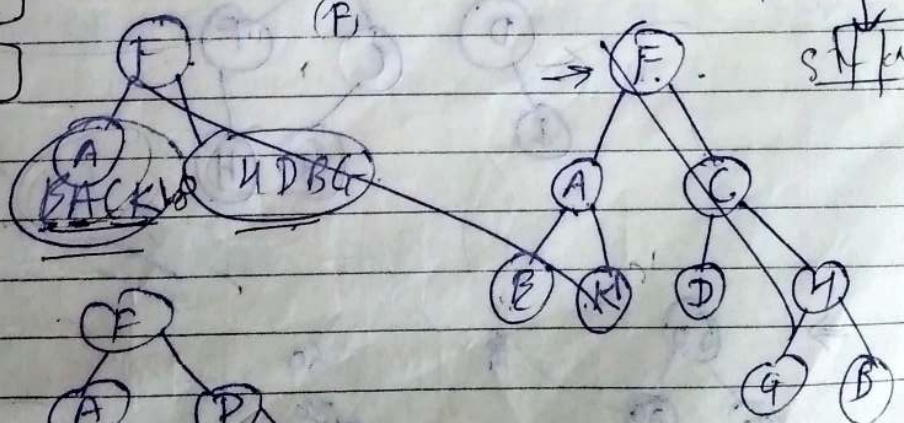
① preorder :- F A E K C D H G B

ini = BACK

prel = A E K C

ini = D H G B

P

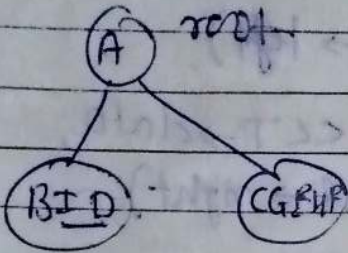


In: 0 1 2 3 4 5 6 7 8
 (2) B I D A C G E H F

C=9

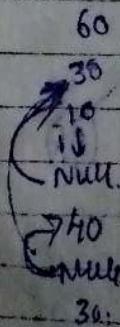
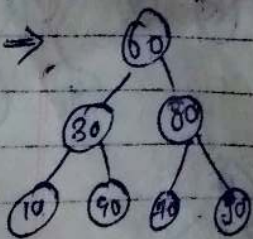
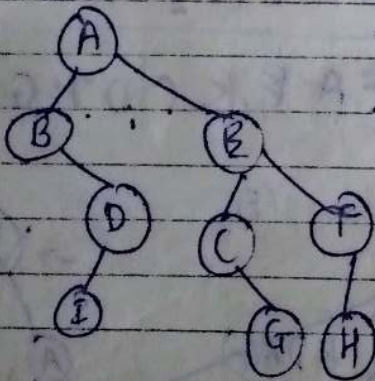
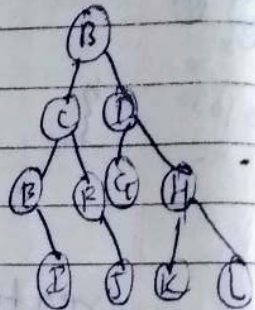
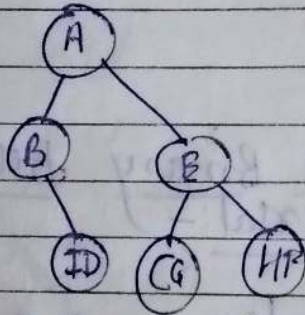
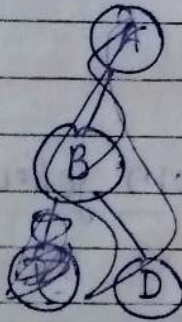
Post: I D B G C H F E A

⇒



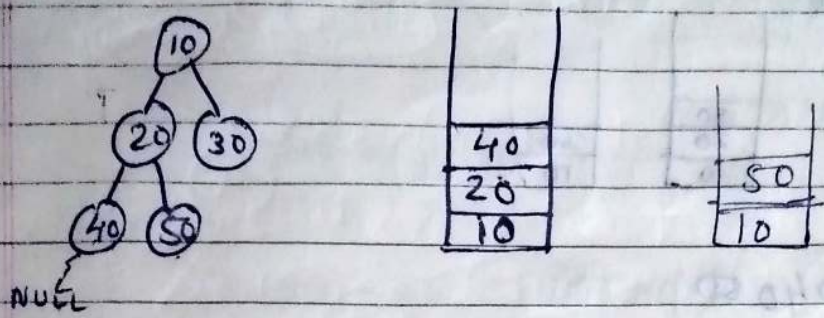
Inorder: (3) E I C F J B G D K H L

Post: I E J F C G K L M D B



collected data
 → Pre (tree → 100%)
 → Post (tree → 100%)

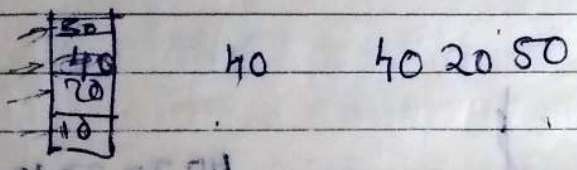
* Binary traversal using non-Recursion method:



① preorder :- 10 20 40 50 30

10 20 40 50 30

② Inorder :- 40 20 50 10 30



root = root -> rptr.

```
void inorder (tree * root)
{
    if (root != NULL)
        inorder (root -> lptr);
    cout << "in" << root->data;
    inorder (root -> rptr);
}
```

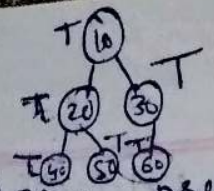
10: 40 20 50 10 30

20
40
NULL

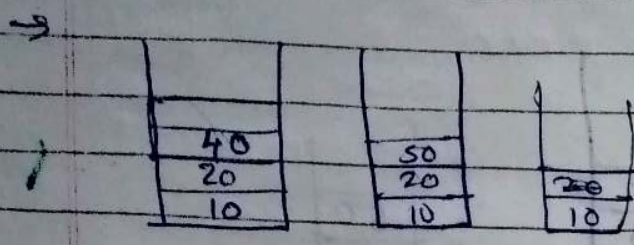
chara in [37];

cm >> in;

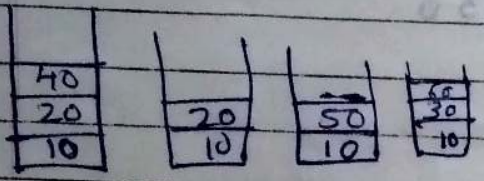
8999099937



* Non-Recursive ~~preorder~~ preorder :-

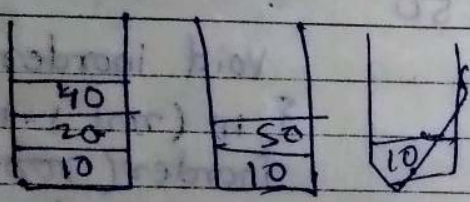


10 20 40 50



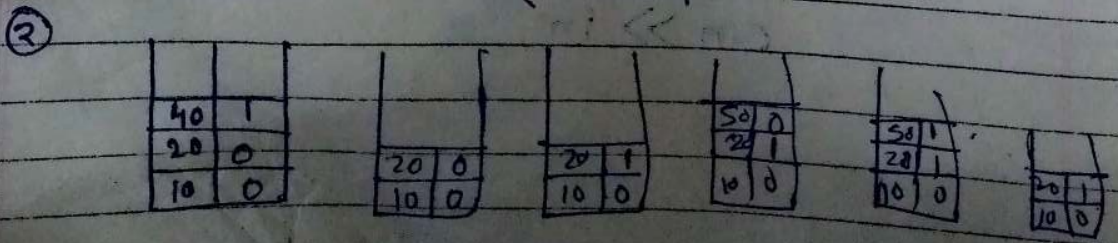
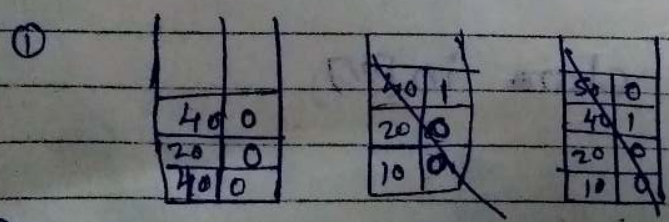
10 20 40 50 30 60

* Inorder :-



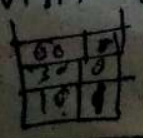
40 20 50 10 60 30

* post order :-



Visit 40.

Visit 50 Visit 20

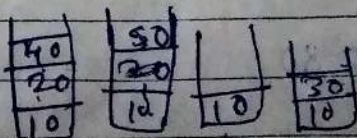
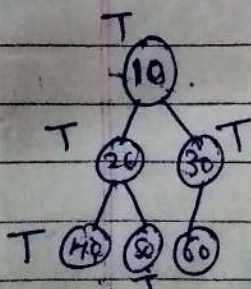


* Non-recursive preorder :-

```

void preorder_nonrec (node * tree *T)
{
    stack s;
    while (T != NULL)
    {
        cout << 'n' << T->data;
        s.push(T);
        T = T->lptr;
    }
    while (!s.empty())
    {
        T = s.pop();
        T = T->rptr;
        while (T != NULL)
        {
            cout << "n" << T->data;
            s.push(T);
            T = T->lptr;
        }
    }
}
    
```

10 20 40 50 30 60



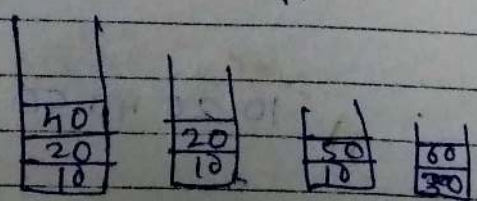
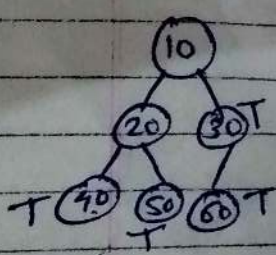
10 20 40 50 30 60

T=40 T=20 T=10

* Non-recursive Inorder :-

```

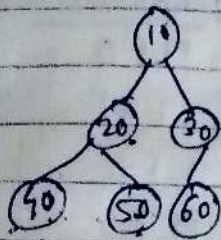
void inorder_nonrec (tree *T)
{
    stack s;
    while (T != NULL)
    {
        s.push(T);
        T = T->lptr;
    }
    while (!s.empty())
    {
        T = s.pop();
        cout << "in" << T->data;
        T = T->rptr;
        while (T != NULL)
        {
            s.push(T);
            T = T->lptr;
        }
    }
}
    
```



40 20 50 10 60 30

Non-recursive post order :-

40 50 20



40	0
20	0
10	0

40	1
20	0
10	0

20	0
10	0

50	0
20	0
10	0

visit 50

50	1
20	0
10	0

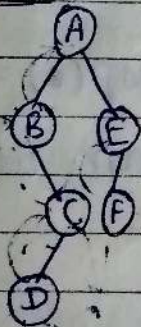
20	0
10	0

20	1
10	0

visit 20

50	1
20	0
10	0

Example :



B	0
A	0

B	1
A	0

D	0
C	0
B	1
A	0

D	1
C	0
B	1
A	0

visit D

C	1
B	1
A	0

visit C

B	1
A	0

visit B

A	0

A	1

visit A

E	0
A	1

F	0
B	0
A	1

F	1
B	0
A	1

E	0
A	1

visit F

B	1
A	1

visit E

visit A

→ DCBFEA

- 1) while going to left, address of the node along with flag=0 is pushed onto the stack.
- 2) During backtracking to traverse the right subtree, an element is popped & if flag is 0 then it is pushed back with flag=1.
- 3) when we return from right subtree, pop & flag=1 then print that node.

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DATE: _____

Non-recursive postorder traversal :-

* \rightarrow while ($T \neq \text{NULL}$)

{

s.push(T); s.push(NULL)

T = T \rightarrow lptr;

}

\rightarrow while (!s.empty())

{

T = s.pop();

\rightarrow check the flag is 0 if (s.pop() = NULL) then push that element again with flag 1.

flag = 1.

{ & s.push(T); s.push((node *) 1);

T = T \rightarrow right.

while (T \neq NULL)

{

if flag = 0; s.push(NULL);
s.push(T);

T = T \rightarrow lptr;

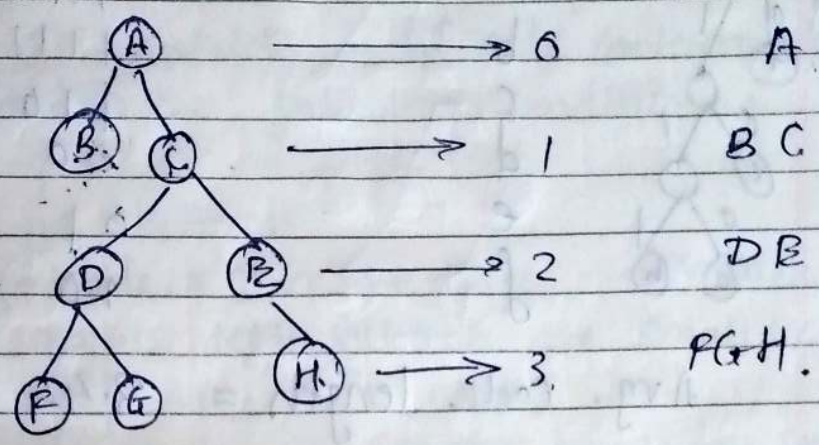
}

\rightarrow else, if when flag = 1

pop & print the data

\rightarrow end

* Binary tree traversal (BFS) :-
 Breadth first traversal.



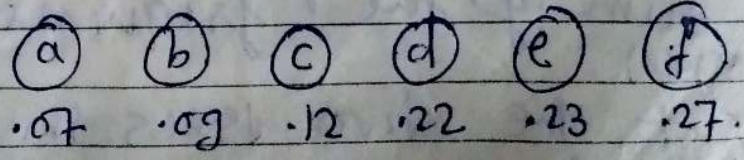
* Huffman algorithm :

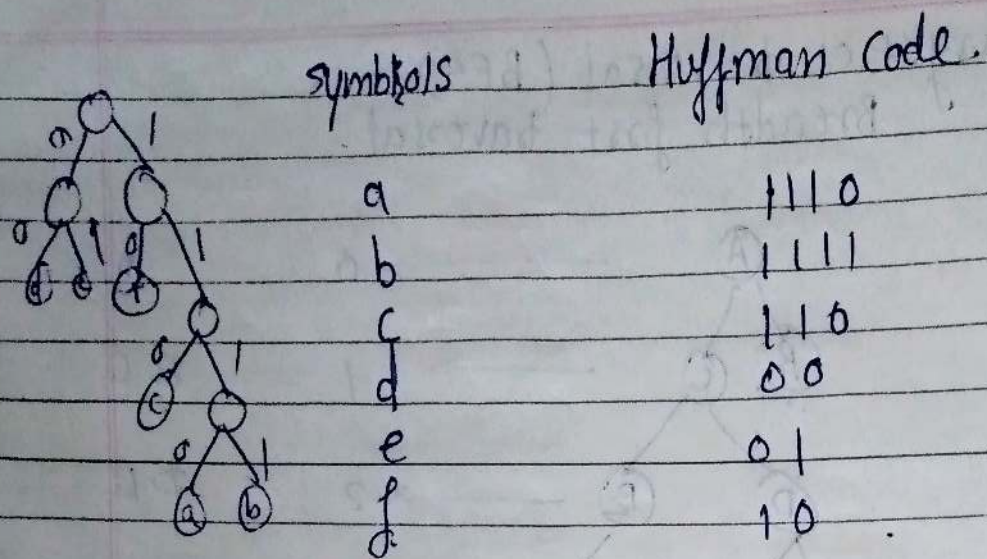
Huffman coding :-

example :-

Suppose character a, b, c, d, e, f have probabilities .07, .09, .12, .22, .23, .27 resp. Find an optimal Huffman code and draw Huffman tree. What is the average code length?

⇒ ①





Avg. code length = 3.44 bits.

Q2) a = 0.4, b = 0.2, c = 0.35, d = 0.05.
 Find Huffman code & draw Huffman tree.
 What is the code length?

→

a	0
b	10
c	110
d	111

Algorithm:-

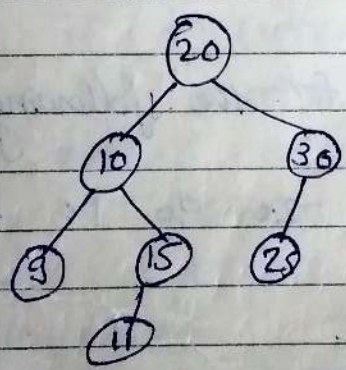
- ① Each character is converted into a single node tree. Each node is labeled by its frequency.
- ② The weight of the tree is equal to sum of the frequencies of its leaves.
- ③ select the two trees in the forest that have smallest weights. Combine these two trees into one. weight of the combined tree = sum of the weights of the two trees.

* Binary Search Tree (BST) :-

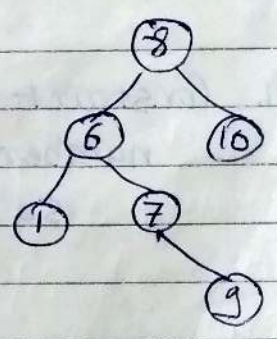
A binary search tree is a binary tree, which is either empty or in which each node contains a key that satisfies the following conditions:

- 1) All keys are distinct.
- 2) For every node x , in the tree, the values of all the keys in its left subtree are smaller than the key value in ~~the~~ the root.
- 3) For every node x , in the tree, the values of all the keys in its right subtree are larger than the key value in ~~the~~ the root.
- 4) The left or right subtrees are also binary search trees.

Binary Search Tree finds its application in Searching.



It is a BST.



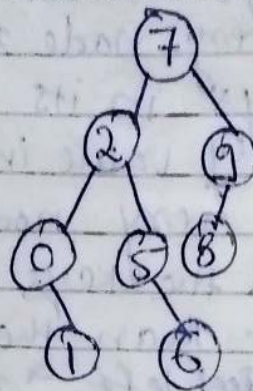
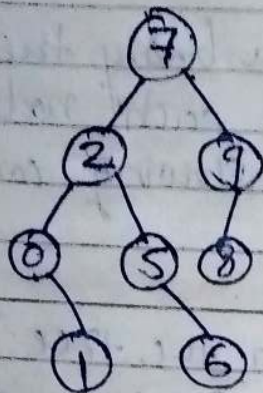
Not a BST.

* Operations of Binary Search Tree :-

① Insert operation :-



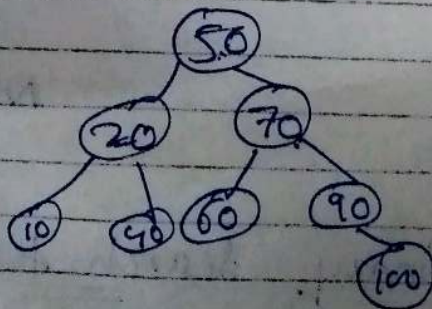
Insert 7, 2, 9, 0, 5, 6, 8, 1. into BST



BST Complexity $\sim O(n \log n)$

Q.1. Construct a BST for the following sequence of numbers :-

50 70 60 20 90 10 40 100

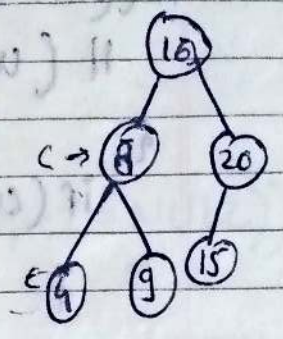


Q.2. 10, 08, 15, 12, 13, 07, 09, 17, 20, 18, 04, 05

② Delete operation :-

```
void BST :: delete (int d)
```

```
{
    int flag = 0;
    if (root == NULL)
        return;
    tree * curr, * parent;
    curr = root;
    while (curr != NULL)
    {
        if (curr->data == d)
        {
            flag = 1;
            break;
        }
        else
        {
            parent = curr;
            if (d > curr->data)
                curr = curr->rptr;
            else
                curr = curr->lptr;
        }
    }
    if (flag == 0)
    {
        cout << "Data not found" << endl;
        return;
    }
}
```



P = 10
4 > 8
④

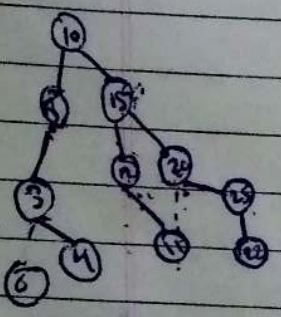
// leaf node deletion.

```
if (curr->lptr == NULL) || (curr->rptr == NULL)
{
    if (parent->lptr == curr)
        parent->lptr = NULL;
    else
        parent->rptr = NULL;
    delete curr;
    return;
}
```

// Node with single child.

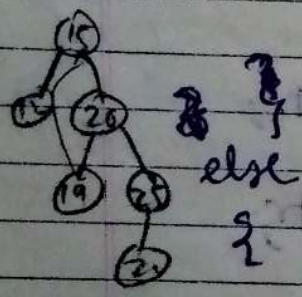
```
if (curr->lptr == NULL && curr->rptr != NULL)
    // (curr->lptr != NULL && curr->rptr == NULL)
```

```
{
    if (curr->lptr == NULL && curr->rptr != NULL)
    {
        if (parent->left == curr)
```



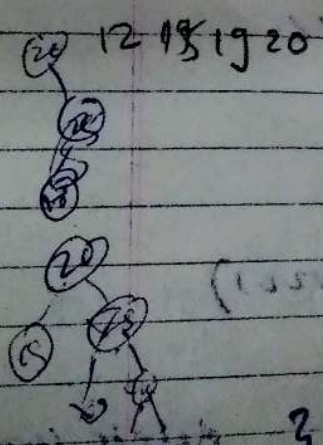
```
{
    parent->left = curr->rptr;
    delete curr;
}
```

```
}
else
{
    parent->rptr = curr->lptr;
    delete curr;
}
```



```
}
else // left child present, no right child.
{
    if (parent->lptr == curr)
```

```
{
    parent->lptr = curr->lptr;
    delete curr;
}
```



```
}
else
{
    parent->rptr = curr->lptr;
    delete curr;
}
```

```
}
return;
}
```

// Node with 2 children

if (curr->lptr != NULL && curr->rptr != NULL)

{

tree * ch;

ch = curr->right;

if ((ch->lptr == NULL && ch->rptr == NULL))

{

curr = ch;

delete ch;

curr->rptr = NULL;

}

else // right child has children

{

~~if (curr->rptr != NULL~~

if ((curr->rptr->lptr != NULL))

{

tree * lcurr, * lcurrp;

lcurrp = curr->rptr;

lcurr = (curr->rptr->lptr);

while (lcurr->left != NULL)

{

lcurrp = lcurr;

lcurr = lcurr->left;

if

curr->data = lcurr->data;

delete lcurr;

lcurrp->left = NULL;

}

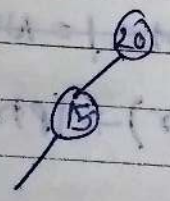
ch = g

16

lcp = 7
lc = 7

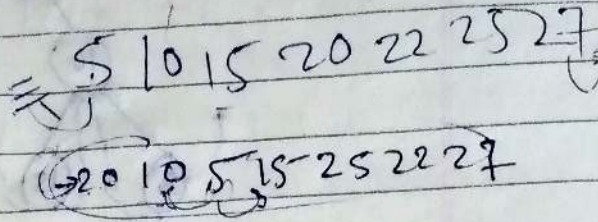
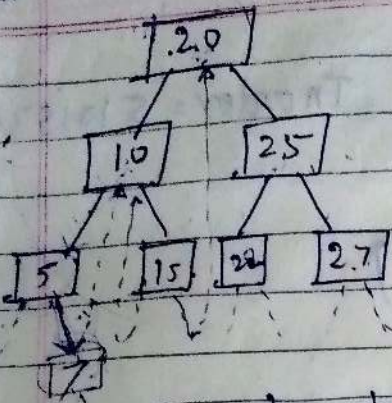
```

    }
    else
    {
        tree_node *temp;
        temp = curr->right; ptr = curr;
        curr->data = temp->data;
        delete temp;
        curr->ptr = temp->ptr;
        delete temp;
    }
}
return;
}
    
```



*

Head



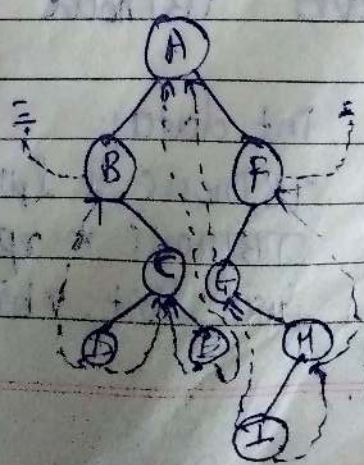
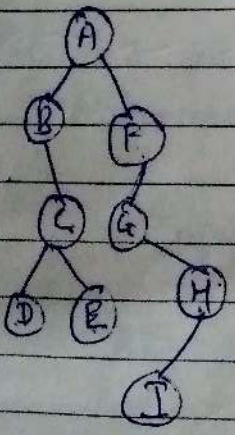
Left Thread	Lptr	Data	Rptr	Rbit Thread
-------------	------	------	------	-------------

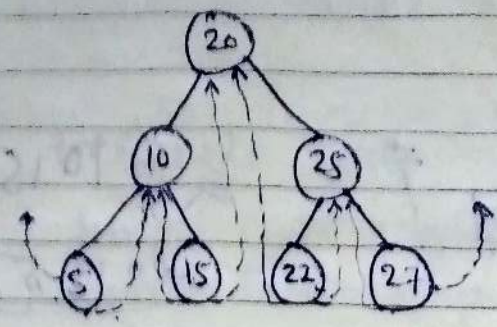
if Lbit & Rbit = 1 then Lptr = Rptr = ptr
 else I threads.

* Threaded Binary Trees (TBT) :-

- In a linked representation of a binary tree, there are more null links than actual pointers.
- These null links can be replaced by pointers, called threads to other nodes.
- A left null link of a node is replaced with the address of its inorder predecessor.
- Similarly a right null link of a node is replaced with the address of its inorder successor.

It is Inorder :- ~~BDC EAGTHF~~
 Inorder :- B D C E A G T H F.



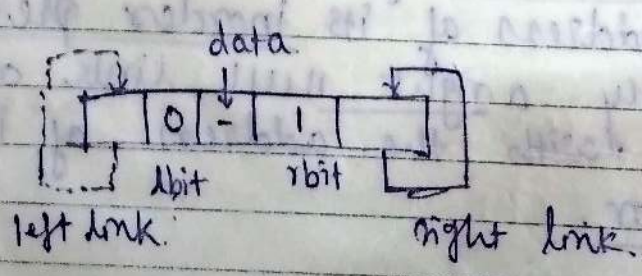


In order = 5 10 15 20 22 25 27

- In Memory representation of a tree node we must be able to distinguish betⁿ threads & normal pointers.
- i.e. Using extra bits rbit & lbit.

$lbit \ \& \ rbit = 1 \rightarrow$ left & right child is normal.

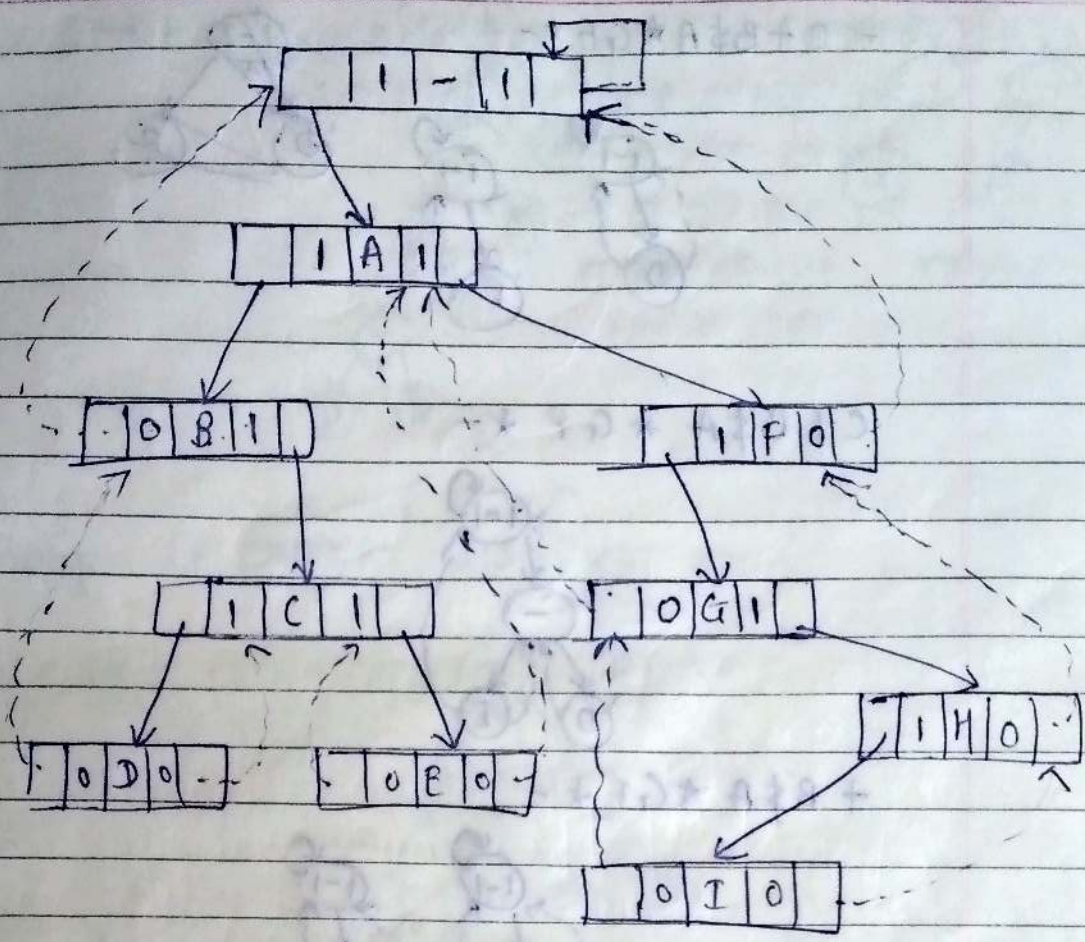
$lbit \ \& \ rbit = 0 \rightarrow$ left & right links are replaced with a thread.



```

class TBTnode
{
    int data;
    TBTnode * lptr;
    TBTnode * rptr;
    int lbit, rbit;
}
    
```





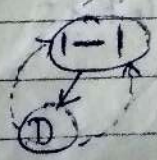
Q: Construct inorder threaded binary tree for the following data:

Inorder: D-E+C\$B*A-G*F
 postorder: DE-C+B\$A*GF*-

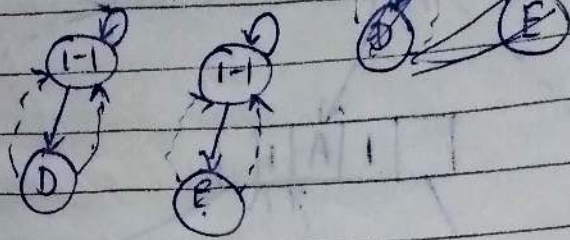
Write its pre-order traversal. Represent Stepwise construction.

→ Inputs

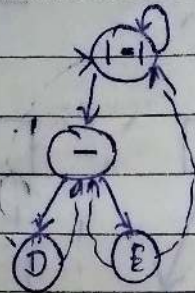
~~DE~~-C+B\$A*GF*-



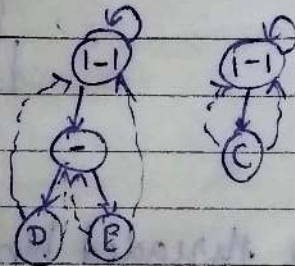
- C + B \$ A * G F * -



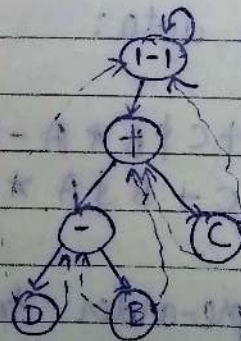
C + B \$ A * G F * -



+ B \$ A * G F * -



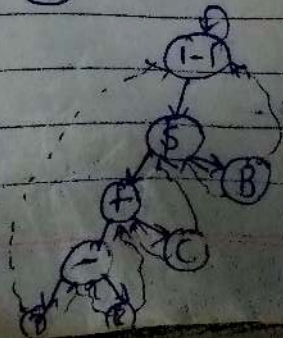
B \$ A * G F * -



\$ A * G F * -



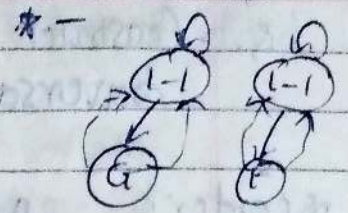
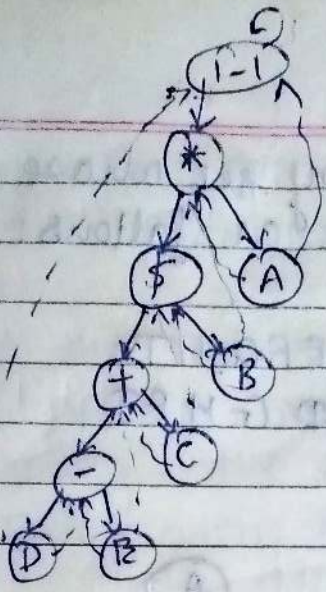
A * G F * -



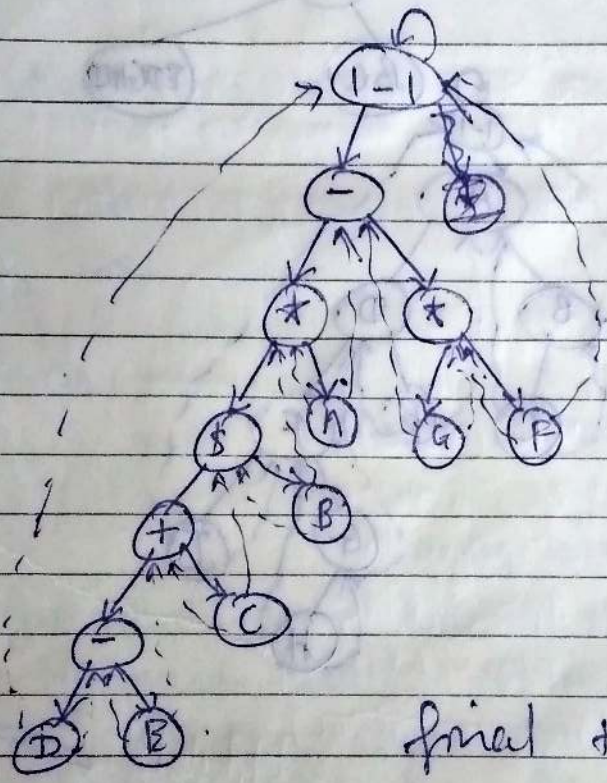
A * G F * -



GFA -



empty.



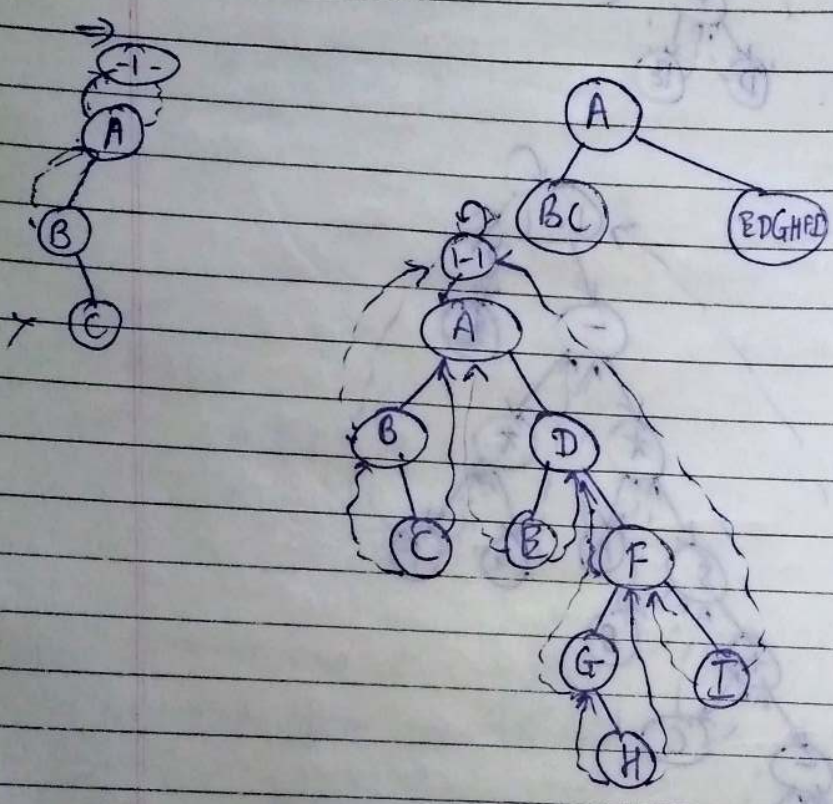
final tree.

pre order: $1-1 * \$ + - D E C B A * G F$



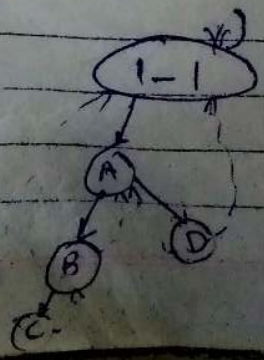
Q. Construct a binary tree whose preorder & inorder traversals are as follows:

Preorder: A B C D E F G H I
 Inorder: B C A E D G H F I



* Preorder traversal (TBT) :-

→ A non-recursive preorder traversal on TBT can be implemented without a stack.

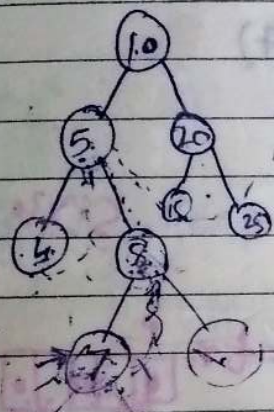


preorder = A B C D

1) If the left child of a node is a normal child then left child is preorder successor.

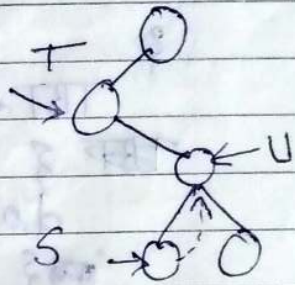
2) If left child of the node is a thread, we can locate the preorder successor by climbing up the tree using the right thread till we reach a node with normal right child.

* Inorder traversal of a TBT:-



4 5 7 8 10 15 20 25

postorder = 4 7 8 5 15 25 20 10



→ If the right child of a node is not a thread then the leftmost child in the right subtree will be the inorder successor.

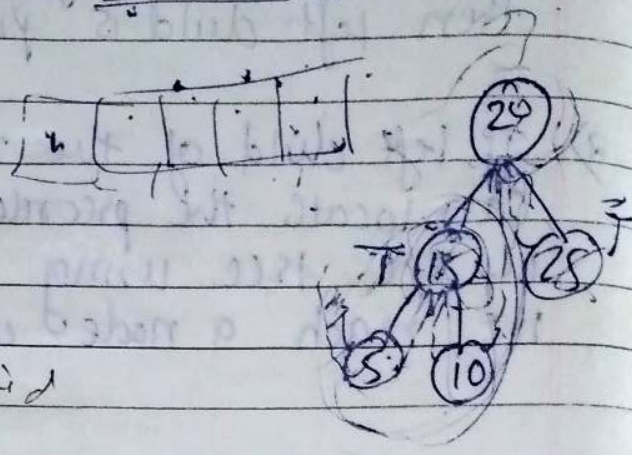
→ If the right link is a thread then the thread itself points to the successor.

* postorder traversal of a TBT:-

* Threaded tree Creation & insertion method :-

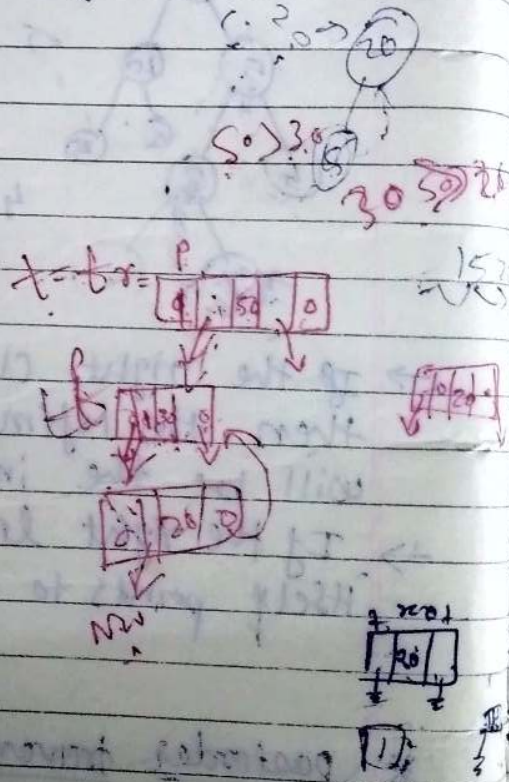
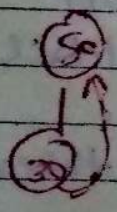
```

class TBT {
    int data;
    TBT * lptr;
    TBT * rptr;
    int lbit, rbit;
public:
    TBT * create (TBT * root)
    {
        TBT * TBT :: create (TBT * root)
    }
}
    
```



```

TBT * TBT :: create (TBT * root)
    {
        do
            {
                P = new (tree);
                cout << "Enter data";
                cin << P->data;
                P->lptr = NULL;
                P->rptr = NULL;
                if (root == NULL)
                    {
                        root = P;
                        root->lbit = 0;
                        root->rbit = 0;
                    }
                else
                    {
                        temp = root;
                        f = 0;
                        while (temp && f == 0)
                            {
                                if (*temp->data > P->data)
                                    {
                                        temp = temp->rptr;
                                        f = 1;
                                    }
                                else
                                    {
                                        temp = temp->lptr;
                                        f = 1;
                                    }
                            }
                    }
            }
        }
    }
}
    
```



```

temp = root;
f = 0;
while (temp && f == 0)
    {
        if (*temp->data > P->data)
            {
                temp = temp->rptr;
                f = 1;
            }
        else
            {
                temp = temp->lptr;
                f = 1;
            }
    }
}
    
```



```
{  
    if ( temp -> lbit == 1 )  
        temp = temp -> lptr;  
    else if ( temp -> lbit == 0 )  
    {  
        temp -> lbit = 1;  
        p -> lbit = 0;  
        p -> rbit = 0;  
        p -> lptr = temp -> lptr;  
        p -> rptr = temp;  
        temp -> lptr = p;  
        f = 1;  
        p -> data = 0;  
    }  
}
```

20
15

```
if ( temp -> data < p -> data )  
    {  
        if ( temp -> rbit == 1 )  
            temp = temp -> rptr;  
        else if ( temp -> rbit == 0 )  
        {  
            temp -> rbit = 1;  
            p -> lbit = 0;  
            p -> rbit = 0;  
            p -> rptr = temp -> rptr;  
            p -> lptr lptr = temp;  
            temp -> rptr = p;  
            f = 1;  
            p -> data = 1;  
        }  
    }  
}
```

```
    cout << " do you want to add more nodes: ";  
    c = getch();  
} while ( c == 'r' || c == 'y' );  
return ( root );  
}
```

```
void TBT :: pre(TBT * root)
```

```
{
```

```
    TBT * temp;
```

```
    temp = root;
```

```
    root = root -> lptr;
```

```
    int flag = 1
```

```
    while (1)
```

```
    {
```

```
        cout << temp -> data;
```

```
        while (temp -> lbit == 1)
```

```
        { temp = temp -> lptr;
```

```
          cout << temp -> data;
```

```
        }
```

```
        flag = 1;
```

```
        while (temp -> rbit rptr != NULL)
```

```
        {
```

```
            if (temp -> rbit == 0)
```

```
                temp = temp -> rptr;
```

```
            else
```

```
            {
```

```
                temp = temp -> rptr;
```

```
                flag = 0;
```

```
                break;
```

```
            }
```

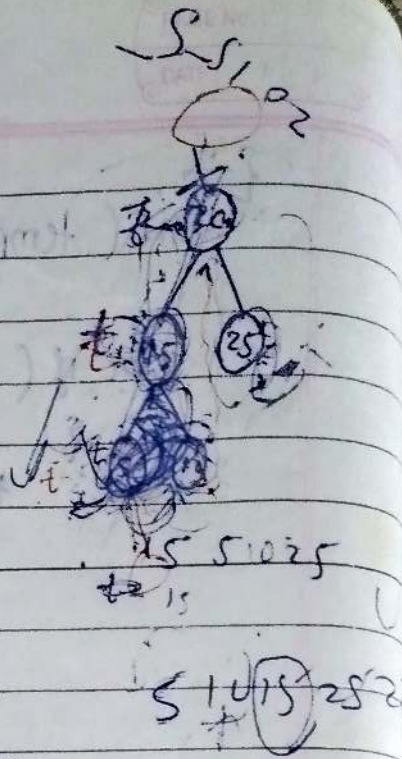
```
        }
```

```
        if (flag == 1)
```

```
            break;
```

```
    }
```

```
}
```



void TBT :: In (TBT *root)

```
{
    temp = root;
    write(1);
    while (temp->lbit == 1)
        temp = temp->lptr;
```

cout << temp->data;

flag = 1;

```
while (temp->rptr != NULL)
```

```
{
```

```
    if (temp->rbit == 0)
```

```
    {
```

```
        temp = temp->rptr;
```

```
        cout << temp->data;
```

```
    }
```

```
    else
```

```
        temp = temp->optr;
```

```
        flag = 0;
```

```
        break;
```

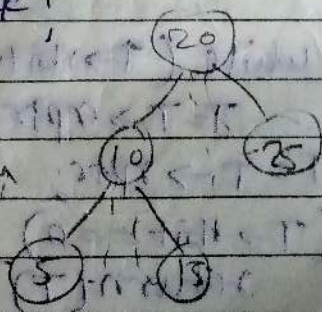
```
    }
```

```
}
```

```
if (flag == 1)
    break;
```

```
}
```

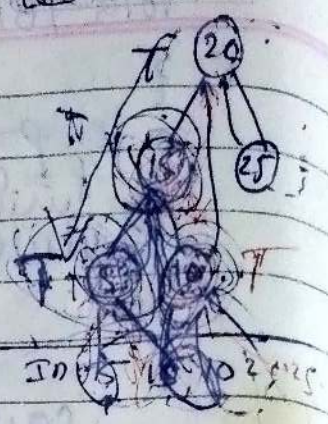
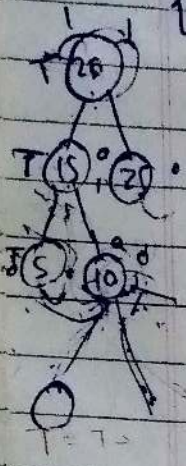
```
}
```



pre :- 20 10 5 15 25

post 5 10 15 25 20

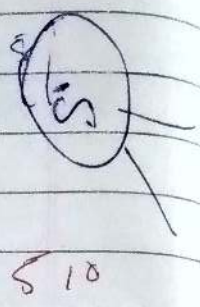
```
void TBT :: post(TBT * root)
```



```

TBT * temp; *T;
T = temp = root;
while (T->lbit == 1 || T->rbit == 1)
{
    if (T->lbit == 1)
        T = T->lptr;
    else
        T = T->rptr;
}
while (T != root)
{
    cout << " " << T->data;
    T = post_scc(T);
}
cout << " \n" << root->data;

```



// function for post order successor of a node.

```
TBT * post_scc(TBT * root)
```

child = 1
right child
0 = left child

```

{
    if (T->child == 1)
    {
        while (T->lbit == 1)
            T = T->lptr;
        return (T->lptr);
    }
    else
    {
        while (T->rbit == 1)
            T = T->rptr;
        T = T->rptr;
        if (T->rbit == 0)
            return (T);
    }
}

```

// locate parent of T when it is left child

```

{
    T = T->rptr;
    while (T->lbit == 1 || T->rbit == 1)
    {
        if (T->lbit == 1)
            T = T->lptr;
        else
            T = T->rptr;
    }
    return (T);
}

```

* Applications of tree :-

↳ Game tree :-

→ one of the most important application of trees is Game tree:

→ Games like tic-tac-toe, chess, 8-puzzle checkers, 16-puzzle checkers etc. are solved by constructing the game tree.

for example 8-puzzle problem.

2	8	3
1	6	4
7	-	5



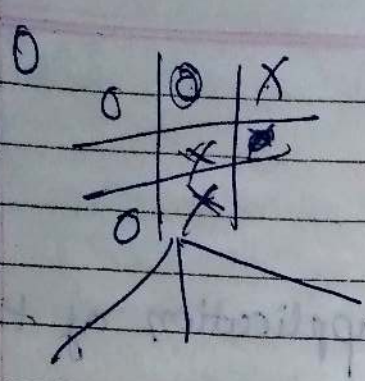
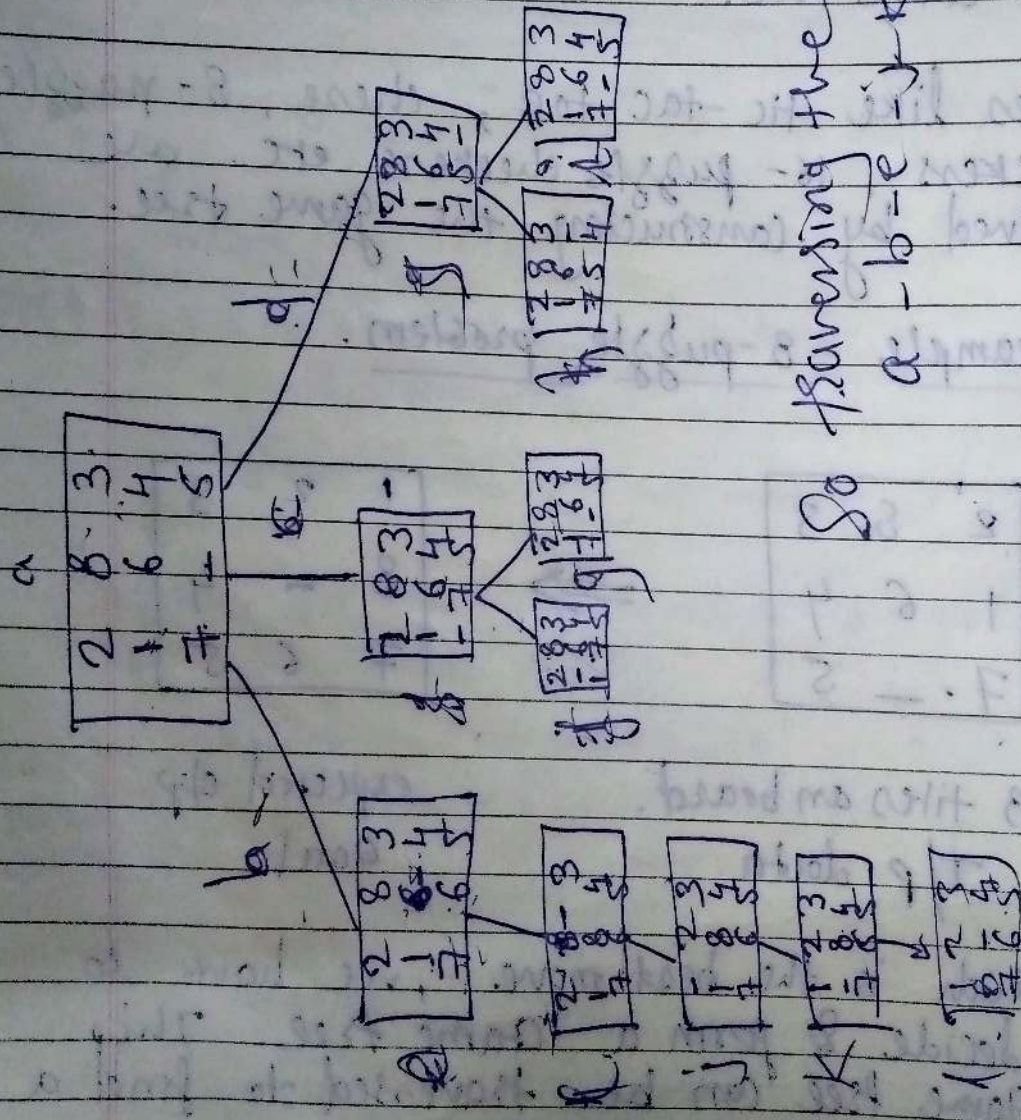
1	2	3
8	-	4
7	6	5

8 tiles on board.
I/p data.

expected o/p.
Goal.

which is the best move, we have to decide & form a game tree. This game tree can be traversed to find a goal ~~state~~ of the problem.





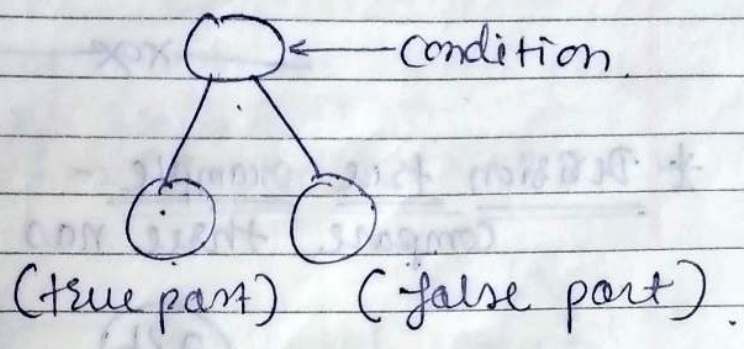
So traversing the path a-b-e-j-k-l is lead to goal state.

② Decision tree :-

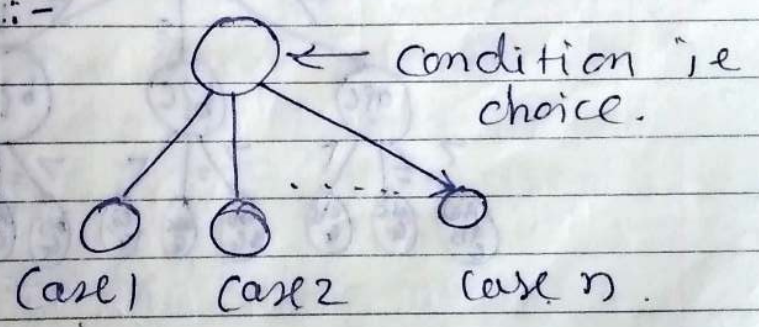
- Imp. application is decision making.
- Most of the program involve conditional stmt rather than just i/p & o/p.

for example :-

① If clause :-



② switch case :-



adv :-

- 1) It provide a mechanism for visualizing the code execution.
- 2) It also provides the framework to analyse how general of algorithm work.

③ Expression trees:-

→ Traversals in expression trees will give you the result of postfix, infix & prefix.

→ Etree consist of operands & operations. where operands are leaves of a tree.

xxx

* Decision tree example:-
 Compare three nos a, b, c

