

NFA - Introduction

NFA - Non-deterministic Finite Automata



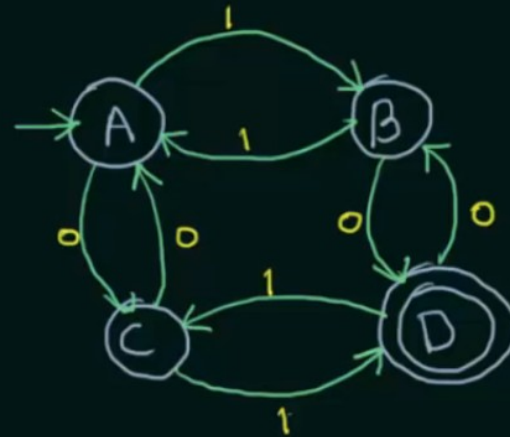
NFA - Non-deterministic Finite Automata

Deterministic Finite Automata



DETERMINISM

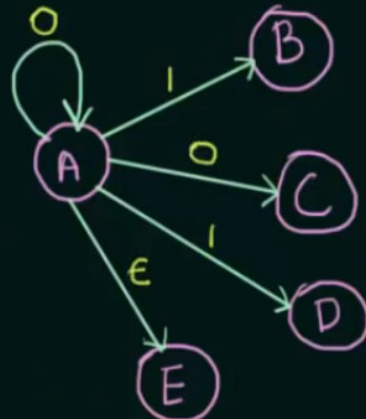
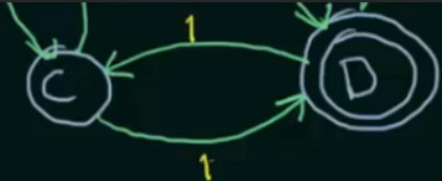
- >> In DFA, given the current state we know what the next state will be
- >> It has only one unique next state
- >> It has no choices or randomness
- >> It is simple and easy to design



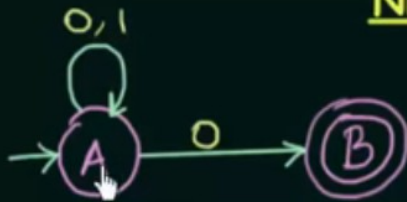
» It has only one unique next state
» It has no choices or randomness
» It is simple and easy to design

Non-deterministic Finite Automata
↓
NON-DETERMINISM

» In NFA, given the current state there could be multiple next states
» The next state may be chosen at random
» All the next states may be chosen in parallel



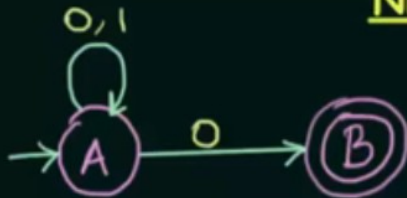
NFA - Formal Definition



$L = \{ \text{Set of all strings that end with 0} \}$




NFA - Formal Definition



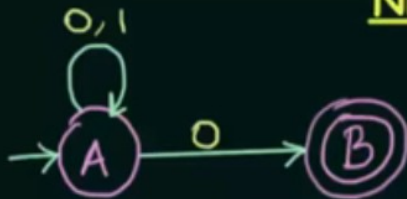
$L = \{ \text{Set of all strings that end with 0} \}$

$(Q, \Sigma, q_0, F, \delta)$

$Q =$ 



NFA - Formal Definition



$L = \{ \text{Set of all strings that end with 0} \}$

$(Q, \Sigma, q_0, F, \delta)$

$Q =$ Set of all states

$\Sigma =$ inputs

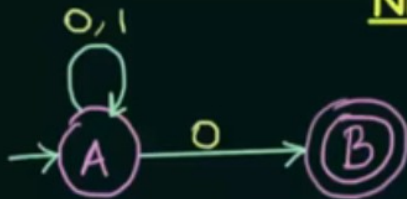
$q_0 =$ start state / initial state

$F =$ Set of final states

$\delta = Q \times \Sigma \rightarrow \underline{\quad}$



NFA - Formal Definition



$L = \{ \text{Set of all strings that end with 0} \}$

$(Q, \Sigma, q_0, F, \delta)$

$Q =$ Set of all states

- $\{A, B\}$

$\Sigma =$ inputs

- $\{0, 1\}$

$q_0 =$ start state / initial state

- A

$F =$ Set of final states

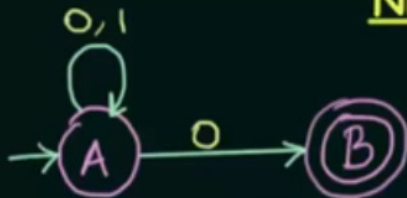
- B

$\delta = Q \times \Sigma \rightarrow _$

- ?



NFA - Formal Definition



$L = \{ \text{Set of all strings that end with 0} \}$

$(Q, \Sigma, q_0, F, \delta)$

$Q =$ Set of all states

$\Sigma =$ inputs

$q_0 =$ start state / initial state

$F =$ Set of final states

$\delta = Q \times \Sigma \rightarrow _$

- $\{A, B\}$

- $\{0, 1\}$

- A

- B

- ?

$A \times 0 \rightarrow A$

$A \times 1 \rightarrow B$

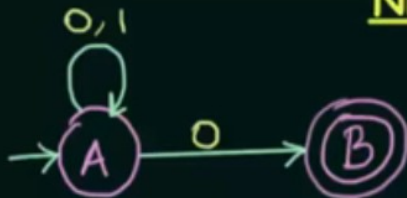
$A \times 1 \rightarrow A$

$B \times 0 \rightarrow \phi$

$B \times 1 \rightarrow \phi$



NFA - Formal Definition



$(Q, \Sigma, q_0, F, \delta)$

Q = Set of all states

Σ = inputs

q_0 = start state / initial state

F = Set of final states

$\delta = Q \times \Sigma \rightarrow _$

$L = \{ \text{Set of all strings that end with 0} \}$

- $\{A, B\}$

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- A

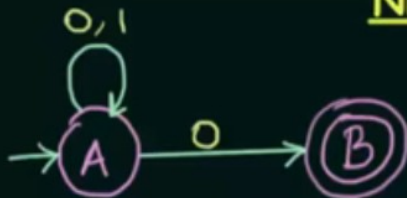
- B

- ?

$A \times 0 \rightarrow A$
 $A \times 0 \rightarrow B$
 $A \times 1 \rightarrow A$
 $B \times 0 \rightarrow \phi$
 $B \times 1 \rightarrow \phi$



NFA - Formal Definition



$(Q, \Sigma, q_0, F, \delta)$

Q = Set of all states

Σ = inputs

q_0 = start state / initial state

F = Set of final states

$\delta = Q \times \Sigma \rightarrow _$

$L = \{ \text{Set of all strings that end with 0} \}$

- $\{A, B\}$

- $\{0, 1\}$

- A

- B

- ?

$A \times 0 \rightarrow A$

$A \times 0 \rightarrow B$

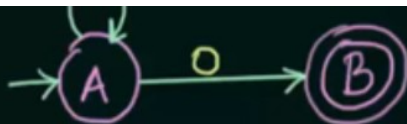
$A \times 1 \rightarrow A$

$B \times 0 \rightarrow \phi$

$B \times 1 \rightarrow \phi$

$A^1 \rightarrow A, B, AB, \phi$





$L = \{ \text{Set of all strings that end with 0} \}$

$(Q, \Sigma, q_0, F, \delta)$

$Q =$ Set of all states

$\Sigma =$ inputs

$q_0 =$ start state / initial state

$F =$ Set of final states

$\delta = Q \times \Sigma \rightarrow _$

- $\{A, B\}$

- $\{0, 1\}$

- A

- B

- ?

$A \times 0 \rightarrow A$

$A \times 0 \rightarrow B$

$A \times 1 \rightarrow A$

$B \times 0 \rightarrow \phi$

$B \times 1 \rightarrow \phi$

$A^1 \rightarrow A, B, AB, \phi$

3 states - A, B, C

$A^1 \rightarrow A, B, C, AB, AC, BC, ABC, \phi$



$(Q, \Sigma, q_0, F, \delta)$

Q = Set of all states

Σ = inputs

q_0 = start state / initial state

F = Set of final states

$\delta = Q \times \Sigma \rightarrow \underline{Q^Q}$

- $\{A, B\}$

- $\{0, 1\}$

- A

- B

- ?

$A \times 0 \rightarrow A$

$A \times 0 \rightarrow B$

$A \times 1 \rightarrow A$

$B \times 0 \rightarrow \phi$

$B \times 1 \rightarrow \phi$

$A^1 \rightarrow A, B, AB, \phi$ - $2^2 - 4$

3 states - A, B, C

$A^1 \rightarrow A, B, C, AB, AC, BC, ABC, \phi$
 $2^3 - 8$



• **Questions????**